

Для следующей ЗЛП построить двойственную задачу. Доказать, что вектор  $x$  является оптимальным вектором исходной задачи. Найти оптимальный вектор двойственной задачи.

$$1. \quad \begin{cases} \max(8x_1 + 2x_2 + 5x_3 - x_4 + x_5) \\ x_1 + 9x_2 - 7x_3 + 9x_5 \leq 3, \\ 7x_1 + 7x_2 - 9x_3 + x_4 - 7x_5 \geq 4, \\ 8x_1 + 2x_2 + 7x_3 + x_4 - 5x_5 = 5, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (12/7, 1/7, 0, -9, 0) \end{cases}$$

$$2. \quad \begin{cases} \max(-6x_1 + 2x_2 - 6x_3 + 2x_4 - 9x_5) \\ 7x_2 + x_3 + 8x_4 - 8x_5 \leq 8, \\ 2x_1 + 3x_2 + 4x_4 - x_5 \geq 6, \\ -2x_1 - 3x_2 + 2x_3 - 2x_5 = 6, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-11, 0, 0, 9, 8) \end{cases}$$

$$3. \quad \begin{cases} \max(7x_1 + x_2 - 8x_3 - 8x_4 - x_5) \\ 7x_1 - 7x_2 + 3x_3 - 5x_4 - 7x_5 \leq 1, \\ -9x_1 - 7x_2 + 9x_4 - 9x_3 \geq 3, \\ -4x_1 - 7x_3 + x_4 + 7x_5 = 2, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -3/7, 0, 0, 2/7) \end{cases}$$

$$4. \quad \begin{cases} \max(9x_1 - 4x_3 - 9x_4 - 6x_5) \\ 6x_1 + 5x_2 + 6x_3 + 2x_4 - 7x_5 \leq 4, \\ 8x_2 + x_3 - x_4 - 2x_5 \geq 6, \\ 3x_2 + x_3 + x_4 - 2x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-8/15, 3/5, 0, 0, -3/5) \end{cases}$$

$$5. \quad \begin{cases} \max(2x_1 - 6x_2 - 7x_3 + 6x_4 + 6x_5) \\ -4x_1 - 7x_2 - 3x_3 + 7x_4 + 4x_5 \leq 7, \\ 6x_1 + 4x_2 - 3x_3 - 5x_4 - 9x_5 \geq 5, \\ x_1 + 4x_2 - x_4 + 3x_5 = 2, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (13, 0, 6, 11, 0) \end{cases}$$

$$6. \quad \begin{cases} \max(-3x_1 - 2x_2 + 7x_3 - 2x_4 - 7x_5) \\ -x_1 + 3x_2 + 5x_3 - 5x_4 + 2x_5 \leq 9, \\ 3x_1 + 4x_2 - x_3 - 5x_4 - x_5 \geq 3, \\ -x_1 + 3x_3 - 2x_2 - 4x_4 - 3x_5 = 6, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (3/13, 0, 15/13, -9/13, 0) \end{cases}$$

$$7. \quad \begin{cases} \max(2x_1 - x_2 - 9x_3 + 3x_4 + 8x_5) \\ 9x_1 + 6x_2 - 7x_3 - 2x_4 - 6x_5 \leq 4, \\ x_1 + 4x_2 + 2x_3 - x_4 - 6x_5 \geq 1, \\ 6x_1 - 7x_2 - 6x_3 - 4x_4 = 4, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (3, 0, 7/3, 0, 10/9) \end{cases}$$

8.  $\max(9x_1 - 2x_2 + 9x_3 - 6x_4)$
- $$\begin{cases} 7x_1 + 5x_2 + 2x_3 + 4x_4 + 5x_5 \leq 4, \\ 3x_1 - 8x_2 + 3x_3 - 2x_4 + 2x_5 \geq 9, \\ 3x_1 + 2x_2 + 8x_3 - x_4 - 4x_5 = 9, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-13/5, 0, 18/5, 0, 3) \end{cases}$$
9.  $\max(-3x_1 + 2x_2 + 2x_3 - 4x_4 - x_5)$
- $$\begin{cases} 8x_1 + 5x_3 + 3x_4 - 3x_5 \leq 9, \\ 5x_1 + 8x_2 - x_3 + 9x_4 + 2x_5 \geq 8, \\ -8x_2 + 8x_3 + x_4 - 7x_5 = 9, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 6/5, 0, 2/5, -13/5) \end{cases}$$
10.  $\max(-4x_1 + 9x_2 + x_3 + 5x_4 - 9x_5)$
- $$\begin{cases} x_1 + 9x_2 - 7x_3 + 6x_4 + 5x_5 \leq 9, \\ x_1 - 7x_3 - 7x_4 + 7x_5 \geq 5, \\ -9x_1 + 9x_2 - 3x_3 + 5x_4 - 8x_5 = 7, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-17/19, 12/19, 0, 0, 16/19) \end{cases}$$
11.  $\max(-2x_1 - x_2 + 6x_3 + 8x_4 + 2x_5)$
- $$\begin{cases} 3x_2 - 3x_1 + 2x_3 + 2x_4 + 3x_5 \leq 4, \\ 4x_1 + 7x_2 - 3x_3 + 2x_4 + 7x_5 \geq 8, \\ -5x_1 - 7x_2 - 2x_3 - x_4 - 2x_5 = 5, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-4/3, 0, 0, -5, 10/3) \end{cases}$$
12.  $\max(-3x_1 - 4x_2 + x_3 - x_4 - 2x_5)$
- $$\begin{cases} -9x_1 + 4x_2 + 8x_3 + x_4 + 4x_5 \leq 5, \\ 3x_4 - x_2 - 2x_1 - 3x_5 \geq 5, \\ 4x_1 + x_2 + 8x_3 - 8x_4 - 6x_5 = 4, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (2, 0, 5/2, 3, 0) \end{cases}$$
13.  $\max(-2x_1 - 2x_2 - 2x_3 - 6x_4 + 8x_5)$
- $$\begin{cases} -3x_1 + 5x_3 + 8x_4 + 2x_5 \leq 2, \\ -8x_1 + 2x_5 - 6x_3 - 2x_4 \geq 4, \\ -x_1 - 6x_2 + 5x_3 + 4x_4 - 6x_5 = 5, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-2/5, -7/6, 0, 0, 2/5) \end{cases}$$
14.  $\max(2x_1 + 5x_2 - 8x_3 - 6x_4 + x_5)$
- $$\begin{cases} 2x_2 + 3x_3 + 2x_4 - 2x_5 \leq 5, \\ x_1 - 3x_2 + 5x_4 - 9x_5 \geq 8, \\ -9x_1 + 7x_2 + x_3 + 7x_4 + x_5 = 4, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (3/2, 3/4, 0, 7/4, 0) \end{cases}$$
15.  $\max(6x_1 + 3x_2 + 5x_3 + 4x_4 + 9x_5)$
- $$\begin{cases} 4x_2 + 7x_3 + 6x_4 - x_5 \leq 3, \\ -8x_1 + 3x_2 - 4x_3 + x_4 - 5x_5 \geq 1, \\ 2x_1 + 4x_2 + 2x_3 + 5x_4 - 4x_5 = 9, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (9/10, 2/5, 0, 0, -7/5) \end{cases}$$

$$16. \quad \begin{cases} \max(-4x_1 + 6x_2 + 7x_3 - 8x_4 + 5x_5) \\ 2x_2 + 5x_3 - 8x_4 \leq 2, \\ 5x_1 - 2x_2 + 3x_3 + 3x_4 + 4x_5 \geq 6, \\ 6x_1 + 4x_2 + 5x_3 + 9x_4 + 5x_5 = 4, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, -2/3, 2/3, 0, 2/3) \end{cases}$$

$$17. \quad \begin{cases} \max(8x_1 + 8x_2 + 7x_3 + 4x_4 + 8x_5) \\ 5x_1 + x_2 + 2x_3 + 2x_4 \leq 6, \\ 6x_1 - 6x_3 + 3x_4 - 9x_5 \geq 1, \\ -2x_1 - 2x_2 + 4x_3 - 4x_4 = 8, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (5/2, 17/6, 0, -14/3, 0) \end{cases}$$

$$18. \quad \begin{cases} \max(-2x_1 + 9x_2 + x_3 - 6x_4 - 2x_5) \\ -9x_1 + 6x_2 + 3x_3 + 6x_4 + x_5 \leq 5, \\ x_1 + x_3 - 5x_4 - x_5 \geq 1, \\ 2x_1 + 8x_2 + 3x_3 + 6x_4 + 7x_5 = 4, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-1/9, 1/9, 10/9, 0, 0) \end{cases}$$

$$19. \quad \begin{cases} \max(-6x_1 - 9x_2 + 3x_3 - x_4 - 3x_5) \\ -6x_1 + 6x_2 - x_3 - 3x_4 + 2x_5 \leq 3, \\ -2x_1 + 5x_2 - 7x_3 - 8x_4 + x_5 \geq 4, \\ -4x_1 + 6x_2 - x_3 - 4x_4 + 6x_5 = 9, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (3/4, 7/8, 0, 0, 9/8) \end{cases}$$

$$20. \quad \begin{cases} \max(-x_1 - 2x_2 - 9x_3 + x_4 - 9x_5) \\ 2x_1 - 8x_2 - 6x_3 - 6x_4 + 4x_5 \leq 6, \\ x_1 - 6x_2 - 6x_4 + 6x_5 \geq 6, \\ -8x_1 - 5x_2 - 7x_3 - 2x_4 + x_5 = 6, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -6, 2, 5, 0) \end{cases}$$

$$21. \quad \begin{cases} \max(-3x_1 + 2x_4 + 6x_5) \\ 5x_1 - 6x_2 - 5x_3 + 8x_4 \leq 2, \\ -2x_2 - 4x_4 - 3x_5 \geq 3, \\ 5x_1 - 3x_2 - 5x_3 - 7x_4 = 2, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (2/5, 0, 0, 0, -1) \end{cases}$$

$$22. \quad \begin{cases} \max(x_1 - 3x_2 + 9x_3 - 8x_5) \\ 4x_2 + 5x_3 + 5x_4 + 6x_5 \leq 6, \\ 8x_2 + x_3 + 9x_4 \geq 4, \\ -5x_1 + 3x_2 + 6x_3 - 9x_4 - 5x_5 = 2, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (9/10, 7/18, 8/9, 0, 0) \end{cases}$$

$$23. \quad \begin{cases} \max(8x_1 + 6x_2 - 3x_3 + 4x_4 + 6x_5) \\ 3x_4 - 9x_2 - x_1 + x_5 \leq 2, \\ -7x_1 - 8x_2 + 3x_3 - 3x_4 - 8x_5 \geq 9, \\ -5x_1 + 5x_2 + 6x_3 - 7x_4 + x_5 = 6, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (8/5, -7/5, 0, -3, 0) \end{cases}$$

24.  $\max(-4x_1 - 6x_2 + 5x_3 + x_4 + 3x_5)$   

$$\begin{cases} -9x_1 - 7x_2 + 4x_4 + 6x_5 \leq 7, \\ -3x_1 - 9x_2 - 6x_3 - 3x_4 \geq 5, \\ -2x_1 + 6x_2 + x_4 + 3x_5 = 6, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (1, 0, -4/3, 0, 8/3) \end{cases}$$
25.  $\max(-9x_1 - x_2 + 4x_3 + 8x_4 - 4x_5)$   

$$\begin{cases} -6x_1 + 2x_2 - 3x_3 + 5x_4 + 3x_5 \leq 2, \\ -8x_1 - 4x_2 - 5x_4 + 6x_5 \geq 1, \\ -7x_1 + 7x_2 + 5x_3 - x_4 + 7x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 0, 1/8, 1/4, 3/8) \end{cases}$$
26.  $\max(-6x_1 + 4x_2 + 8x_3 - 8x_4 - 9x_5)$   

$$\begin{cases} 8x_1 - 2x_2 + 6x_3 - 4x_4 \leq 8, \\ 2x_1 - 8x_2 - 6x_3 + 2x_4 + 3x_5 \geq 4, \\ x_1 - 9x_2 - 6x_3 - 5x_4 - 6x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (3, 0, 0, 4, -10/3) \end{cases}$$
27.  $\max(5x_1 - 7x_2 + 9x_3 + 6x_4 - 6x_5)$   

$$\begin{cases} -2x_1 + 7x_2 + 9x_3 + 4x_4 \leq 5, \\ -9x_1 - 7x_2 - 5x_4 + x_5 \geq 3, \\ -x_1 - 2x_2 + 9x_3 - 2x_4 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (1, 0, 7/9, 0, 12) \end{cases}$$
28.  $\max(7x_1 + 6x_2 - 9x_3 + 7x_4 - 4x_5)$   

$$\begin{cases} -x_1 - 3x_2 + 3x_3 + x_4 - 6x_5 \leq 3, \\ -5x_1 + 3x_2 - x_3 - 5x_4 - x_5 \geq 9, \\ 2x_1 + 9x_2 + 2x_3 + 4x_5 = 4, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (10, 0, 0, -11, -4) \end{cases}$$
29.  $\max(-2x_1 - x_2 + 9x_3 - 3x_4 + 7x_5)$   

$$\begin{cases} 2x_1 - 3x_2 + 6x_3 - x_4 + 4x_5 \leq 7, \\ 5x_2 + 3x_3 + 8x_4 \geq 2, \\ -6x_1 + 8x_2 - 3x_3 + 8x_4 - 3x_5 = 2, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-11/10, 2/5, 0, 0, 13/5) \end{cases}$$
30.  $\max(5x_1 + 4x_2 - 4x_3 + 6x_4 - 9x_5)$   

$$\begin{cases} 3x_1 + 6x_2 - 3x_3 - 6x_5 \leq 4, \\ -8x_1 + 7x_2 - 9x_3 - 5x_5 \geq 8, \\ -9x_1 - x_2 - 8x_3 - 6x_4 - 2x_5 = 5, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, 7/3, 0, -16/9, 5/3) \end{cases}$$
31.  $\max(8x_1 + 4x_2 - 9x_3 - 3x_4 - 6x_5)$   

$$\begin{cases} -3x_2 - 8x_3 + 7x_4 + 3x_5 \leq 8, \\ 4x_3 - 4x_4 + 4x_5 \geq 8, \\ 2x_1 + 2x_2 + 4x_3 - 5x_4 + 4x_5 = 6, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (7, -8, 2, 0, 0) \end{cases}$$

$$\begin{aligned}
& \max(4x_1 - 3x_2 + 2x_4 - 5x_5) \\
32. \quad & \begin{cases} 2x_1 - x_2 - 3x_3 + 5x_4 + 7x_5 \leq 9, \\ -x_2 - 3x_3 + 2x_4 + 3x_5 \geq 4, \\ 8x_1 + 2x_2 - 6x_3 - x_4 + 5x_5 = 4, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (5/2, -6, 2/3, 0, 0) \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \max(-3x_1 - 4x_2 + 5x_3 + 4x_4 + 5x_5) \\
33. \quad & \begin{cases} -5x_1 + 2x_2 - 7x_3 + 4x_4 - 7x_5 \leq 5, \\ -4x_1 + 2x_2 - 7x_3 + 2x_4 - 4x_5 \geq 7, \\ -9x_1 + 3x_2 - 9x_3 + 5x_4 + 5x_5 = 2, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (19/8, 8, 0, 0, -1/8) \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \max(-2x_1 + 3x_4 - 4x_5) \\
34. \quad & \begin{cases} 9x_1 - 5x_2 + 4x_3 + 8x_4 - 7x_5 \leq 7, \\ -9x_1 - 2x_2 + 5x_3 - 8x_4 - 9x_5 \geq 7, \\ 9x_1 - x_2 + 4x_3 + x_4 - 9x_5 = 5, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -2/5, 8/5, 0, 1/5) \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \max(9x_1 - 4x_2 - 9x_3 + 2x_4 - 2x_5) \\
35. \quad & \begin{cases} -3x_1 + x_2 + 6x_3 - 4x_4 + x_5 \leq 1, \\ 7x_2 + 3x_3 - 2x_4 - 3x_5 \geq 3, \\ x_1 + 6x_2 + 4x_3 + 9x_4 - 3x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (6, 6, 0, 0, 13) \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \max(3x_1 - 6x_3 + 4x_4 - x_5) \\
36. \quad & \begin{cases} -3x_1 + 9x_2 + 2x_3 - 4x_4 + 6x_5 \leq 5, \\ -x_1 + 9x_3 - 2x_4 + 3x_5 \geq 3, \\ 7x_1 - 3x_2 - x_3 + 9x_4 - 6x_5 = 7, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (1, 0, 0, 8/5, 12/5) \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \max(-4x_1 - 8x_2 + 3x_3 - 7x_4 - x_5) \\
37. \quad & \begin{cases} 5x_2 + 3x_3 - 4x_4 - x_5 \leq 8, \\ 7x_1 + 8x_2 + x_3 + x_4 - x_5 \geq 9, \\ x_1 - 3x_2 + 4x_3 - 5x_4 - x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-2, 0, 0, 3, -20) \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \max(-8x_1 - 8x_3 - 5x_4 - 2x_5) \\
38. \quad & \begin{cases} 4x_1 - 6x_2 + 9x_3 - x_4 + 3x_5 \leq 4, \\ -9x_1 - 6x_2 + 9x_3 + 3x_4 + 3x_5 \geq 6, \\ -9x_1 - 2x_2 + 7x_3 - 6x_4 + 2x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 3/2, 0, 1/2, 9/2) \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \max(-5x_1 - 5x_2 + 4x_3 - 6x_4 + 2x_5) \\
39. \quad & \begin{cases} -9x_1 - 5x_2 + 6x_3 + 3x_4 + 4x_5 \leq 3, \\ -3x_1 - 5x_2 - 7x_3 - 9x_4 + 8x_5 \geq 1, \\ x_1 + 6x_2 - 9x_3 + 2x_4 - 2x_5 = 9, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-1, 2, 0, 0, 1) \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \max(-9x_1 + 3x_2 - 8x_3 - 4x_4 + 8x_5) \\
40. \quad & \begin{cases} x_1 - 6x_2 + 6x_3 - 4x_4 + 5x_5 \leq 9, \\ -4x_1 - 7x_2 + 9x_3 + x_5 \geq 8, \\ 8x_1 - 9x_2 - 3x_3 - x_4 - 3x_5 = 4, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (1, 0, 4/3, 0, 0) \end{cases} \\
& \max(-8x_1 - 6x_2 + 3x_3 + 6x_4 + 2x_5) \\
41. \quad & \begin{cases} -7x_1 - 2x_2 + 2x_3 + 8x_4 + 8x_5 \leq 2, \\ 6x_1 + 2x_3 - 3x_4 - 6x_5 \geq 6, \\ -3x_1 - 7x_2 - 7x_3 + 4x_4 + 8x_5 = 6, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (14/5, 0, 0, 9/5, 9/10) \end{cases} \\
& \max(-4x_1 - 8x_2 + 9x_3 + 7x_4 - 6x_5) \\
42. \quad & \begin{cases} 2x_1 + 3x_2 + 3x_3 + 3x_4 - 7x_5 \leq 5, \\ -8x_1 + x_2 - 6x_3 + 7x_4 \geq 6, \\ 2x_1 - x_3 - 2x_4 - 3x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (5/2, 0, -2, 2, 0) \end{cases} \\
& \max(5x_1 - 9x_2 - 8x_3 - 6x_4 - 2x_5) \\
43. \quad & \begin{cases} -9x_1 + 9x_2 - 8x_3 + 6x_4 + 4x_5 \leq 2, \\ -7x_1 - 2x_2 - 6x_3 + 3x_4 + 3x_5 \geq 2, \\ -5x_1 + 5x_2 - 4x_4 + 3x_5 = 7, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-2, 0, 3/2, 0, -1) \end{cases} \\
& \max(7x_2 - x_3 - 8x_4 - 2x_5) \\
44. \quad & \begin{cases} 6x_1 - 7x_2 + 9x_3 + 7x_4 + 4x_5 \leq 5, \\ 4x_1 - 7x_2 + 9x_4 \geq 7, \\ 3x_1 - 9x_2 + 8x_4 - 5x_5 = 2, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (3/5, 7/5, 0, 8/5, 0) \end{cases} \\
& \max(-7x_1 + 7x_2 + 5x_3 - 7x_4 - 5x_5) \\
45. \quad & \begin{cases} 3x_1 - x_3 - x_4 + 6x_5 \leq 5, \\ 6x_1 - 5x_2 - 6x_3 + 6x_4 + 9x_5 \geq 6, \\ 2x_1 - x_3 - 7x_4 + 8x_5 = 7, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -3/5, 1, 0, 1) \end{cases} \\
& \max(-5x_3 - 5x_4 - 5x_5) \\
46. \quad & \begin{cases} -7x_1 + 6x_2 - 6x_3 - 5x_5 \leq 5, \\ 4x_1 + 4x_2 + 3x_3 + 2x_4 + 3x_5 \geq 9, \\ 9x_1 + 2x_2 + x_3 + 3x_4 + 9x_5 = 6, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (1/4, 13/8, 1/2, 0, 0) \end{cases} \\
& \max(-5x_1 + x_2 - 3x_3 + 6x_4 + x_5) \\
47. \quad & \begin{cases} 7x_1 - x_2 + 7x_3 - x_4 + 3x_5 \leq 5, \\ 4x_1 - x_2 - 7x_3 - 4x_4 + 3x_5 \geq 9, \\ 6x_1 + x_2 - 5x_3 + x_5 = 2, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, 7/12, 0, -4/3, 17/12) \end{cases}
\end{aligned}$$

$$48. \quad \begin{cases} \max(-6x_2 - 2x_3 + 4x_4 + 3x_5) \\ -3x_1 + 6x_3 + 7x_4 - x_5 \leq 1, \\ -4x_1 - x_2 + 4x_3 - 6x_4 - 3x_5 \geq 5, \\ 9x_1 - x_2 + 6x_4 = 5, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, -5, 3/14, 0, 2/7) \end{cases}$$

$$49. \quad \begin{cases} \max(-9x_1 + 5x_2 + 9x_3 + x_4 - 6x_5) \\ -3x_1 + 3x_2 + 6x_3 - 3x_4 + 7x_5 \leq 5, \\ -6x_1 + 9x_3 - 9x_4 - 9x_5 \geq 6, \\ 2x_1 + 6x_2 + x_3 - 2x_4 + 9x_5 = 6, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (5, -4/3, 4, 0, 0) \end{cases}$$

$$50. \quad \begin{cases} \max(6x_1 + 8x_2 - 7x_3 + 9x_4 - 5x_5) \\ -x_1 + 2x_2 + 7x_3 - 2x_5 \leq 6, \\ 6x_1 - 4x_2 + 5x_3 - 6x_4 + x_5 \geq 7, \\ 5x_1 - 4x_2 + 6x_3 + 7x_4 + 2x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (1, -3/2, 0, 0, -5) \end{cases}$$

$$51. \quad \begin{cases} \max(-7x_3 + 4x_4 + 4x_5) \\ 2x_1 + 8x_2 + x_3 + 5x_4 - x_5 \leq 3, \\ 7x_2 - 3x_3 - 8x_4 + 4x_5 \geq 6, \\ 4x_1 + 2x_2 - 3x_3 - 7x_4 + 3x_5 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 0, -9/2, 15/8, 15/8) \end{cases}$$

$$52. \quad \begin{cases} \max(9x_1 + 7x_2 + 3x_3 + 5x_4 - 6x_5) \\ 7x_1 + 6x_2 + 4x_3 - x_4 - 5x_5 \leq 4, \\ 9x_1 + 5x_2 - 2x_3 - 6x_4 - 8x_5 \geq 3, \\ 4x_1 - 5x_2 + x_4 - 6x_5 = 8, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-3/11, 0, 0, 10/11, -15/11) \end{cases}$$

$$53. \quad \begin{cases} \max(-2x_1 - 2x_2 - 8x_3 - 4x_4 + x_5) \\ -6x_1 - 6x_2 - 4x_3 + 6x_4 + 9x_5 \leq 7, \\ 2x_1 + x_2 - 4x_3 + 5x_4 + 5x_5 \geq 9, \\ 7x_1 + 3x_2 - 4x_3 + 3x_4 + 5x_5 = 5, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 2/3, 5/4, 8/3, 0) \end{cases}$$

$$54. \quad \begin{cases} \max(3x_1 + x_2 + x_3 + 5x_4 - 9x_5) \\ -2x_1 + x_2 - 3x_3 + 4x_4 + 8x_5 \leq 7, \\ 2x_1 - 9x_2 + 3x_3 - 9x_4 + 4x_5 \geq 3, \\ -5x_1 + 9x_2 - 7x_3 - 2x_4 + x_5 = 7, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (3, -5/4, -19/4, 0, 0) \end{cases}$$

$$55. \quad \begin{cases} \max(-3x_1 + 8x_2 - x_3 - 6x_4 - 8x_5) \\ x_1 + 2x_2 + 4x_3 + 3x_4 - 6x_5 \leq 1, \\ 6x_1 + 3x_2 - 2x_3 - 6x_4 - 9x_5 \geq 6, \\ 6x_1 + 5x_2 - 9x_3 - x_4 + x_5 = 8, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (1, 3/8, 0, 0, 1/8) \end{cases}$$

$$56. \quad \begin{cases} \max(-8x_1 - 9x_2 - 4x_3 - x_5) \\ 3x_1 + 5x_2 + 5x_3 + 2x_4 - 6x_5 \leq 1, \\ 7x_1 - 9x_2 + 6x_3 - 3x_5 \geq 5, \\ 7x_1 - 3x_2 + 9x_3 - 2x_4 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (3/4, 0, 0, -3/8, 1/12) \end{cases}$$

$$57. \quad \begin{cases} \max(x_1 - 5x_2 - 6x_3 + 5x_4 + 2x_5) \\ 7x_1 - 5x_2 - 7x_3 + 5x_4 + 7x_5 \leq 9, \\ 3x_1 - 9x_2 - 9x_3 - 7x_4 + 7x_5 \geq 7, \\ -4x_1 + 8x_3 - 8x_5 = 8, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -12/5, 1, 4/5, 0) \end{cases}$$

$$58. \quad \begin{cases} \max(-x_1 - x_2 + 7x_3 - 3x_4 + 7x_5) \\ -3x_1 + x_2 + 4x_3 + 7x_4 + 2x_5 \leq 4, \\ -8x_1 + 4x_2 - 7x_3 - 4x_4 + x_5 \geq 1, \\ -5x_1 - x_2 + 4x_3 + 5x_4 - 3x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, 7/4, 1, -1/4, 0) \end{cases}$$

$$59. \quad \begin{cases} \max(-3x_1 + 2x_2 + 2x_3 - 3x_5) \\ -3x_1 - x_2 - 3x_3 + 9x_4 + 3x_5 \leq 1, \\ -x_1 - x_2 + 5x_3 - 2x_4 \geq 6, \\ 2x_1 + 3x_2 + 7x_3 - 8x_4 + 7x_5 = 2, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -1, 15/13, 5/13, 0) \end{cases}$$

$$60. \quad \begin{cases} \max(7x_1 - 2x_2 - 4x_4 + 8x_5) \\ 8x_1 + x_2 + 2x_3 + x_4 + x_5 \leq 5, \\ -4x_1 + 5x_2 - 6x_4 + 7x_5 \geq 9, \\ -x_1 - 2x_2 + 3x_3 - 4x_5 = 1, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, 4/3, 5/3, 0, 1/3) \end{cases}$$

$$61. \quad \begin{cases} \max(-x_1 + x_2 + x_3 + 4x_4 - 7x_5) \\ 5x_1 - 5x_2 - 5x_3 + x_4 + 4x_5 \leq 9, \\ 6x_1 - 3x_2 - 9x_3 - 9x_4 - x_5 \geq 4, \\ 7x_1 + x_2 - x_3 - 2x_4 + 8x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 13/6, -7/2, 7/3, 0) \end{cases}$$

$$62. \quad \begin{cases} \max(-7x_2 + 5x_4 - 6x_5) \\ -2x_1 + 2x_3 + 2x_4 - 3x_5 \leq 2, \\ -8x_1 + x_2 + 3x_3 - x_4 + 2x_5 \geq 8, \\ -6x_1 - 2x_2 + 7x_3 - 3x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-19/20, 0, 0, 7/5, 9/10) \end{cases}$$

$$63. \quad \begin{cases} \max(-8x_1 - 9x_2 - 2x_3 - 4x_4 + 5x_5) \\ -9x_1 - 8x_2 - 8x_3 + 6x_4 + 6x_5 \leq 3, \\ 4x_1 - 4x_2 - 5x_3 + 2x_4 - 6x_5 \geq 6, \\ 7x_1 - 8x_2 - 8x_3 + 7x_4 - 8x_5 = 8, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (0, 9/14, -9/7, 0, -5/14) \end{cases}$$



$$64. \quad \begin{cases} \max(-2x_1 - 6x_2 - 7x_3 - x_4 - 4x_5) \\ \begin{cases} 9x_1 - 9x_2 + 9x_3 - 2x_4 - 7x_5 \leq 6, \\ x_1 - 9x_2 - 4x_4 - 8x_5 \geq 9, \\ -4x_1 - 6x_2 - 6x_3 - 2x_4 - 2x_5 = 6, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \end{cases} \\ x = (0, -5/9, 0, -5/3, 1/3) \end{cases}$$

$$65. \quad \begin{cases} \max(6x_1 + 2x_2 - 8x_3 - 4x_4 - 2x_5) \\ \begin{cases} 2x_1 + 2x_2 + 5x_3 + 7x_4 + 6x_5 \leq 2, \\ 5x_1 - 4x_2 + 6x_3 - 8x_4 + 3x_5 \geq 5, \\ -x_1 + x_2 - 8x_3 - 5x_4 + x_5 = 5, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \end{cases} \\ x = (-13/2, -6, 0, 0, 9/2) \end{cases}$$

$$66. \quad \begin{cases} \max(-5x_1 + 3x_2 - 8x_3 + 5x_4 + x_5) \\ \begin{cases} -2x_1 - 4x_3 + 3x_4 + 4x_5 \leq 3, \\ -5x_1 - 2x_2 + 2x_3 - 6x_4 + 9x_5 \geq 4, \\ -4x_1 - 2x_2 - 9x_3 - x_4 - 7x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \end{cases} \\ x = (0, -2, 0, 9/17, 6/17) \end{cases}$$

$$67. \quad \begin{cases} \max(3x_1 + 4x_2 - x_3 + 2x_4 - 5x_5) \\ \begin{cases} -6x_1 + 9x_2 + 3x_3 + 3x_4 + x_5 \leq 1, \\ 3x_1 - 5x_2 - 9x_3 + x_4 + 4x_5 \geq 1, \\ -6x_1 + 4x_2 + 6x_3 - 5x_4 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \end{cases} \\ x = (2/3, 0, 1, 0, 2) \end{cases}$$

$$68. \quad \begin{cases} \max(9x_1 - 6x_2 - 5x_3 - 9x_4 - 4x_5) \\ \begin{cases} 5x_1 - 6x_2 + 9x_3 + 8x_4 - 7x_5 \leq 5, \\ -4x_1 + 2x_2 - 9x_3 + 2x_4 - 6x_5 \geq 5, \\ 9x_1 - 2x_2 + 2x_3 + 6x_4 - 4x_5 = 9, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \end{cases} \\ x = (2/7, 3/2, 0, 11/7, 0) \end{cases}$$

$$69. \quad \begin{cases} \max(6x_1 + 4x_2 + 4x_3 + 6x_4 - 4x_5) \\ \begin{cases} 7x_1 + 6x_3 + 9x_4 + 8x_5 \leq 8, \\ -6x_1 - 5x_2 + 4x_3 - x_4 - 4x_5 \geq 2, \\ -x_1 + 2x_2 - 4x_3 - 9x_4 + 8x_5 = 4, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \end{cases} \\ x = (0, -8/9, 2/9, 0, 5/6) \end{cases}$$

$$70. \quad \begin{cases} \max(3x_1 - 3x_2 - 8x_3 + 8x_4) \\ \begin{cases} -5x_1 - x_2 + 4x_3 + 8x_4 + 8x_5 \leq 4, \\ -3x_1 - 2x_2 - 8x_3 - 2x_4 + 5x_5 \geq 1, \\ -2x_1 + 3x_2 - 8x_3 - 4x_4 + 2x_5 = 4, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \end{cases} \\ x = (6/5, 6/5, 0, 0, 7/5) \end{cases}$$

$$71. \quad \begin{cases} \max(-6x_1 - 4x_2 - x_3 - 2x_4 - 6x_5) \\ \begin{cases} x_1 + 2x_2 - 6x_3 + 6x_4 + 5x_5 \leq 8, \\ x_2 - 6x_3 + 2x_4 - 2x_5 \geq 7, \\ 6x_1 + 5x_2 - 3x_3 - 7x_4 + 3x_5 = 9, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \end{cases} \\ x = (2/3, 1/3, -10/9, 0, 0) \end{cases}$$

$$72. \quad \begin{cases} \max(-9x_2 + 2x_3 - 2x_4 - 6x_5) \\ -2x_1 - 4x_2 - x_3 + 3x_4 - 8x_5 \leq 7, \\ -2x_1 - 9x_2 - 8x_3 - 4x_5 \geq 2, \\ -2x_1 + 2x_2 - 9x_3 + 5x_4 - 6x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-1, 0, 1/3, 0, -2/3) \end{cases}$$

$$73. \quad \begin{cases} \max(-6x_2 + x_3 - 5x_4 + 2x_5) \\ 9x_1 - x_4 \leq 8, \\ -2x_1 - 7x_2 + 5x_3 - 4x_4 + 2x_5 \geq 6, \\ 8x_1 - 5x_2 - 3x_3 + x_4 - 2x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 0, -8, -8, 7) \end{cases}$$

$$74. \quad \begin{cases} \max(-5x_1 - 9x_2 + 4x_3 - x_4 + 5x_5) \\ -2x_3 + 6x_4 + 7x_5 \leq 9, \\ -5x_1 - 6x_2 + 6x_5 \geq 3, \\ 2x_1 - 9x_2 - 4x_3 + 6x_4 - x_5 = 9, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 0, -2, 1/4, 1/2) \end{cases}$$

$$75. \quad \begin{cases} \max(-4x_1 - 7x_2 + 2x_3 - 5x_4 - x_5) \\ 3x_1 + 2x_2 + x_3 - 6x_4 - 6x_5 \leq 3, \\ -3x_1 + 4x_2 + x_3 - 4x_4 - 4x_5 \geq 2, \\ -6x_1 + 7x_2 + 2x_3 + 8x_4 - 7x_5 = 4, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (1/6, 0, 5/2, 0, 0) \end{cases}$$

$$76. \quad \begin{cases} \max(-5x_1 + 5x_2 - 9x_3 - 5x_4 - x_5) \\ -2x_1 - 6x_2 - 2x_4 - 2x_5 \leq 2, \\ 9x_1 - 4x_2 - 5x_3 - 2x_4 + 5x_5 \geq 4, \\ 8x_1 + 2x_2 - 3x_3 - x_4 + 3x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, 2/9, 0, -17/9, 2/9) \end{cases}$$

$$77. \quad \begin{cases} \max(-3x_1 + 6x_2 + 6x_3 + 8x_4 + 8x_5) \\ 3x_1 - 9x_2 + 2x_3 + 2x_4 + 3x_5 \leq 8, \\ -5x_1 - 9x_2 - 2x_4 - 8x_5 \geq 6, \\ -2x_1 - 6x_2 - 6x_4 = 4, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -2/3, 1, 0, 0) \end{cases}$$

$$78. \quad \begin{cases} \max(8x_1 + 7x_2 - 7x_3 - 9x_4 + 8x_5) \\ 4x_1 - 4x_2 + 2x_3 + 2x_4 - x_5 \leq 2, \\ -2x_1 + 2x_2 - 8x_3 - 2x_5 \geq 5, \\ -2x_1 + 5x_2 + 2x_3 - 2x_4 - x_5 = 4, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (7/6, 11/3, 0, 6, 0) \end{cases}$$

$$79. \quad \begin{cases} \max(-4x_1 + 3x_2 + 6x_3 - 2x_5) \\ 7x_1 + 9x_2 + x_3 + 7x_4 - 6x_5 \leq 9, \\ -5x_1 - 5x_2 + x_4 - x_5 \geq 1, \\ -7x_1 - 8x_2 - 5x_3 + 9x_4 + 2x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 7/4, 5/4, 1/4) \end{cases}$$

$$80. \begin{cases} \max(8x_1 - 2x_2 - x_3 - 9x_4 - 2x_5) \\ 7x_2 - 4x_3 + 3x_4 + 8x_5 \leq 8, \\ -7x_1 - 5x_2 + x_3 - 4x_4 + 7x_5 \geq 5, \\ -2x_1 - 9x_2 - 9x_3 + 7x_4 + 8x_5 = 9, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (1/8, 0, -1/4, 0, 7/8) \end{cases}$$

$$81. \begin{cases} \max(6x_1 + 2x_2 - 9x_3 + x_4 + 6x_5) \\ 4x_1 - 5x_2 - 9x_3 + 8x_4 + 4x_5 \leq 5, \\ -7x_1 + 7x_2 - x_3 - 2x_4 - 6x_5 \geq 4, \\ -6x_1 - 4x_2 + 4x_4 - 7x_5 = 6, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, 5/3, 4/3, 19/6, 0) \end{cases}$$

$$82. \begin{cases} \max(-7x_1 - 7x_3 - 7x_4 - 5x_5) \\ 6x_1 + 4x_3 - 9x_4 - 3x_5 \leq 2, \\ 2x_1 + 4x_2 - 4x_3 - 6x_4 + 9x_5 \geq 9, \\ 4x_1 + 4x_2 - 3x_3 + 3x_4 + 6x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, 1/12, 0, -4/9, 2/3) \end{cases}$$

$$83. \begin{cases} \max(5x_1 - 9x_2 - 6x_3 - 8x_4 + 3x_5) \\ -9x_1 - 3x_2 - 6x_3 - 9x_4 + 9x_5 \leq 9, \\ -2x_1 + 9x_2 + 5x_3 + 9x_4 + x_5 \geq 4, \\ -7x_1 - 5x_2 - 3x_3 - 7x_4 - 3x_5 = 4, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 3, 0, -5/2, -1/2) \end{cases}$$

$$84. \begin{cases} \max(-5x_1 - 9x_2 - 6x_3 - 3x_4 - 4x_5) \\ -4x_1 - 4x_2 + 2x_3 + 4x_4 - 6x_5 \leq 3, \\ 2x_1 + 5x_2 + 8x_3 + 6x_4 \geq 9, \\ 8x_1 + 9x_2 + 5x_3 + 5x_4 - 4x_5 = 8, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 9/2, -9/2, -2) \end{cases}$$

$$85. \begin{cases} \max(2x_1 - 3x_2 - 5x_3 - 2x_4 - 5x_5) \\ -9x_1 + x_2 + 2x_3 - x_4 + 9x_5 \leq 2, \\ -6x_1 + 3x_2 - 3x_4 - x_5 \geq 3, \\ 6x_1 + x_2 - 6x_3 - 3x_4 - 2x_5 = 1, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-1/9, 0, 1/9, -7/9, 0) \end{cases}$$

$$86. \begin{cases} \max(-8x_1 + 3x_2 - 9x_3 - 4x_4 - 9x_5) \\ 4x_1 + 6x_2 + 8x_3 + 6x_4 + 5x_5 \leq 2, \\ 8x_1 + 3x_2 - 5x_3 + 5x_4 + 8x_5 \geq 9, \\ 6x_1 - 3x_2 - x_3 + 3x_5 = 9, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (1, -7/11, 0, 0, 4/11) \end{cases}$$

$$87. \begin{cases} \max(7x_1 + 4x_2 - 9x_3 - 6x_5) \\ 5x_1 + 4x_2 + 8x_3 - 8x_4 + 6x_5 \leq 3, \\ 5x_1 + 2x_2 + 4x_3 - 4x_4 - 6x_5 \geq 8, \\ 5x_1 - 2x_2 + 8x_4 - 8x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (13/5, -10, 0, -15/4, 0) \end{cases}$$

$$\begin{aligned}
& \max(-8x_1 - x_2 - 4x_3 + 2x_4 - 3x_5) \\
88. \quad & \begin{cases} 5x_1 - 9x_2 + 9x_3 \leq 9, \\ 9x_1 - 8x_2 - 7x_3 + 6x_4 + 3x_5 \geq 8, \\ 3x_1 - x_2 + 4x_3 + 6x_4 - 3x_5 = 9, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, -1, 0, 2/3, -4/3) \end{cases} \\
& \max(7x_1 - 3x_2 - 7x_3 - 3x_4 - 9x_5) \\
89. \quad & \begin{cases} -2x_1 + 4x_2 + 9x_3 - x_4 + 6x_5 \leq 8, \\ 3x_1 - 2x_2 + 4x_3 + x_4 - 3x_5 \geq 5, \\ 5x_1 - 3x_2 - 2x_3 + 2x_4 - 6x_5 = 3, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (5/3, 4/3, 2/3, 0, 0) \end{cases} \\
& \max(-4x_1 - 3x_2 - 6x_3 + 6x_5) \\
90. \quad & \begin{cases} 5x_1 - 7x_2 - 3x_3 + 4x_4 + 8x_5 \leq 3, \\ 7x_1 - 4x_2 + 3x_3 + 4x_4 - 3x_5 \geq 7, \\ 2x_1 + 9x_2 + 6x_3 + 6x_4 + 2x_5 = 2, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -2/3, 1, 1/3, 0) \end{cases} \\
& \max(2x_1 + 4x_2 + x_3 - x_4 - 7x_5) \\
91. \quad & \begin{cases} -x_1 + 6x_2 + 7x_3 - 2x_4 - 3x_5 \leq 5, \\ -3x_1 - 2x_2 + 9x_3 - 7x_5 \geq 1, \\ -x_1 + 2x_2 + 4x_3 - 5x_4 + 5x_5 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (5/3, 0, 2/3, -1, 0) \end{cases} \\
& \max(8x_1 - 2x_2 + 5x_3 - x_4 + x_5) \\
92. \quad & \begin{cases} -2x_1 + x_2 + x_3 + 8x_4 + 5x_5 \leq 7, \\ -4x_1 + x_2 - 9x_3 + 6x_4 + x_5 \geq 5, \\ -6x_1 + 3x_2 + 3x_3 + 8x_4 + 3x_5 = 4, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-1/16, -13/8, 0, 17/16, 0) \end{cases} \\
& \max(x_1 - 2x_2 + x_3 + 9x_4 - 8x_5) \\
93. \quad & \begin{cases} -6x_1 - 4x_2 + 6x_4 + x_5 \leq 9, \\ -6x_1 + 2x_2 - 6x_3 - 4x_4 - 6x_5 \geq 6, \\ -2x_2 + 4x_3 - 9x_4 + 4x_5 = 6, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-17/6, 2, 5/2, 0, 0) \end{cases} \\
& \max(-x_1 + x_2 - 9x_3 - 9x_4 - 8x_5) \\
94. \quad & \begin{cases} 7x_1 + 4x_2 + 3x_3 + 6x_4 - 8x_5 \leq 5, \\ -9x_1 + 6x_2 + 7x_3 + 4x_4 - 8x_5 \geq 3, \\ 7x_1 + 5x_3 + 6x_4 - 4x_5 = 5, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, -17/15, 1/15, 0, -7/6) \end{cases} \\
& \max(-3x_1 - 3x_2 + 4x_3 + 2x_4 - 4x_5) \\
95. \quad & \begin{cases} 2x_1 + 8x_2 - 9x_3 - 5x_4 + 8x_5 \leq 4, \\ 6x_1 - 9x_3 + 2x_4 - 6x_5 \geq 7, \\ 6x_1 - 4x_2 - 9x_3 + 9x_4 + 7x_5 = 6, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (5/4, 1/4, 1/18, 0, 0) \end{cases}
\end{aligned}$$

$$96. \quad \begin{cases} \max(-6x_1 + 2x_2 - 3x_3 + x_4 + 3x_5) \\ -6x_1 + 6x_2 + 2x_4 + 4x_5 \leq 7, \\ -4x_1 - 4x_2 - 4x_3 - 4x_4 + 3x_5 \geq 2, \\ 6x_1 + 6x_2 - 8x_3 + 5x_4 - 4x_5 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 15/2, 0, -11, -4) \end{cases}$$

$$97. \quad \begin{cases} \max(4x_1 - 3x_2 + 6x_3 - x_4 - 9x_5) \\ 3x_1 + 6x_2 + 6x_3 - 8x_4 - 2x_5 \leq 2, \\ 3x_1 - 3x_2 - 7x_3 - 6x_4 \geq 9, \\ 2x_1 - 5x_2 - 8x_3 - 8x_4 - 2x_5 = 8, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-6, 0, 0, -9/2, 8) \end{cases}$$

$$98. \quad \begin{cases} \max(-3x_1 - 3x_2 - 6x_3 - 7x_4 + 6x_5) \\ -6x_1 + 8x_2 - 2x_3 + 2x_4 - 8x_5 \leq 4, \\ -7x_1 - 7x_2 - 8x_3 + 6x_4 - 2x_5 \geq 4, \\ 4x_1 + 9x_2 - 5x_3 - 2x_4 - 2x_5 = 4, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 3/2, 0, 3, 7/4) \end{cases}$$

$$99. \quad \begin{cases} \max(5x_1 + x_2 - 5x_3 - x_4 + 9x_5) \\ 5x_1 + 4x_2 + 5x_3 + 4x_4 + 5x_5 \leq 6, \\ -4x_1 - 4x_2 + 5x_3 - 2x_4 - 3x_5 \geq 7, \\ -8x_1 - 8x_2 + 7x_4 + 9x_5 = 1, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -1/8, 13/10, 0, 0) \end{cases}$$

$$100. \quad \begin{cases} \max(-3x_1 - 3x_2 - 7x_3 + 5x_5) \\ -2x_1 + 9x_2 + 3x_3 + 8x_4 + 9x_5 \leq 2, \\ -4x_1 - 6x_2 - 3x_3 + 5x_4 + 2x_5 \geq 6, \\ 2x_1 + 9x_2 + 5x_3 - 4x_5 = 4, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-5/2, -7/3, 6, 0, 0) \end{cases}$$

$$101. \quad \begin{cases} \max(-2x_1 + 3x_2 - 2x_3 - 6x_4 - 2x_5) \\ -6x_1 + 8x_2 + 2x_3 - 2x_5 \leq 9, \\ -8x_1 + 4x_2 + 4x_3 + 3x_4 + 4x_5 \geq 9, \\ -6x_1 + 7x_2 - 5x_3 - x_4 + 2x_5 = 9, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 5/4, 1/4, 0, 3/4) \end{cases}$$

$$102. \quad \begin{cases} \max(7x_1 + 2x_2 - x_3 - 7x_4 + 9x_5) \\ -8x_1 + 2x_3 - 3x_4 \leq 4, \\ -6x_1 - x_2 - 7x_3 - 4x_4 - x_5 \geq 1, \\ 3x_1 + 7x_2 + 9x_3 + 4x_4 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-1/2, 9/14, 0, 0, 19/14) \end{cases}$$

$$103. \quad \begin{cases} \max(3x_1 + x_2 - 6x_3 + 3x_4 - 5x_5) \\ 4x_1 + 5x_2 - 6x_3 + 3x_5 \leq 5, \\ -6x_1 + 2x_2 - 5x_4 - 8x_5 \geq 9, \\ -3x_1 + 4x_2 - 4x_3 - 5x_5 = 5, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 5/2, 5/4, -4/5, 0) \end{cases}$$

$$\begin{aligned}
& \max(x_1 - 5x_3 + 3x_4 + 5x_5) \\
104. \quad & \begin{cases} 3x_1 - 9x_2 + 2x_3 + 7x_4 + x_5 \leq 2, \\ x_1 - 3x_2 - x_3 - 5x_4 - x_5 \geq 1, \\ 2x_1 + 2x_3 - 2x_4 - 5x_5 = 5, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (15/8, 3/8, 0, 0, -1/4) \end{cases} \\
& \max(6x_1 + 5x_2 + 9x_3 - 5x_4 + 3x_5) \\
105. \quad & \begin{cases} 4x_1 + 4x_2 - 6x_3 - 4x_4 + 3x_5 \leq 5, \\ 2x_2 - 8x_3 - 4x_4 + 3x_5 \geq 3, \\ 3x_1 + 8x_2 + 2x_3 + x_4 + 3x_5 = 6, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (1/8, 3/4, 0, -3/8, 0) \end{cases} \\
& \max(3x_1 + 9x_2 + 6x_3 + 6x_4 + 6x_5) \\
106. \quad & \begin{cases} -4x_1 - x_2 - 3x_3 - 3x_4 - 5x_5 \leq 5, \\ 8x_1 - 6x_2 + 7x_3 - x_4 + 5x_5 \geq 3, \\ 9x_1 + 9x_2 + 4x_3 + 4x_4 + 5x_5 = 5, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (0, 0, 6, 4, -7) \end{cases} \\
& \max(x_1 + x_2 - 9x_3 + 3x_4 + 3x_5) \\
107. \quad & \begin{cases} x_1 - x_2 - x_3 + 3x_4 - x_5 \leq 3, \\ -4x_1 - 6x_2 - x_3 - 4x_4 \geq 8, \\ -5x_1 - 4x_2 + x_3 + 4x_4 + 3x_5 = 4, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (11/8, -9/4, 0, 0, 5/8) \end{cases} \\
& \max(5x_1 + 4x_2 - 6x_3 - 2x_4 + 5x_5) \\
108. \quad & \begin{cases} x_1 - 5x_2 + x_3 - 2x_4 + 9x_5 \leq 1, \\ -2x_1 - 9x_2 + 2x_3 - 9x_4 + 8x_5 \geq 5, \\ -5x_2 + 2x_3 + x_4 + x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 2/3, 17/5, -7/15, 0) \end{cases} \\
& \max(-3x_1 + 8x_2 + 2x_3 + 3x_4 + 6x_5) \\
109. \quad & \begin{cases} 8x_1 + x_2 + 5x_3 + x_4 + 5x_5 \leq 2, \\ 4x_1 - x_2 - 4x_3 + x_4 - 7x_5 \geq 5, \\ -x_1 - 4x_2 - 3x_4 + 9x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -3, 0, 15/4, 1/4) \end{cases} \\
& \max(-8x_1 - 6x_2 + 6x_3 - 2x_4 - 3x_5) \\
110. \quad & \begin{cases} -6x_1 - 6x_2 + 2x_4 + 3x_5 \leq 1, \\ -2x_1 + 6x_2 - x_3 + 9x_4 + 6x_5 \geq 4, \\ 7x_1 + 9x_2 + 6x_3 + 3x_4 - 6x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-8/5, 1, 0, 0, -13/15) \end{cases} \\
& \max(6x_1 + 5x_2 + 9x_3 + 6x_4 + 3x_5) \\
111. \quad & \begin{cases} -4x_1 + 3x_2 + 5x_5 \leq 4, \\ -4x_1 - x_2 - 5x_3 + 2x_4 - x_5 \geq 7, \\ -x_1 + 2x_2 - 3x_3 + 4x_4 - x_5 = 8, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-1, 0, 1/7, 13/7, 0) \end{cases}
\end{aligned}$$

$$112. \quad \begin{cases} \max(3x_1 + 6x_2 - x_3 - 2x_4 - x_5) \\ 7x_1 + 6x_2 + 5x_3 - 7x_4 + 6x_5 \leq 6, \\ -x_2 + 7x_3 - 7x_4 + 6x_5 \geq 9, \\ -6x_1 - x_2 + x_3 - 3x_4 + 3x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 3/2, 5/2, 8/3) \end{cases}$$

$$113. \quad \begin{cases} \max(8x_1 + x_2 - 6x_3 - 6x_4 - x_5) \\ -x_1 + 2x_2 + 9x_3 - 2x_5 \leq 7, \\ x_1 - 6x_2 + 9x_3 - 7x_4 - 5x_5 \geq 9, \\ 9x_1 - 3x_3 - 3x_4 - 9x_5 = 8, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (7/4, 0, 13/12, 0, 1/2) \end{cases}$$

$$114. \quad \begin{cases} \max(5x_1 - x_2 + 3x_3 - 6x_4 + x_5) \\ x_1 + 3x_2 + x_3 - 5x_4 + x_5 \leq 7, \\ 2x_1 + 5x_2 - 6x_3 - 5x_4 \geq 7, \\ -8x_1 - x_2 + x_3 - 3x_4 + 4x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (8/13, 0, 0, -15/13, 8/13) \end{cases}$$

$$115. \quad \begin{cases} \max(4x_1 + 3x_2 + 2x_3 + 2x_4 + 3x_5) \\ -8x_1 + 2x_2 + 8x_3 + 8x_4 + 2x_5 \leq 6, \\ -x_1 - 6x_2 - 3x_3 + 8x_4 - 8x_5 \geq 7, \\ 9x_1 - 3x_2 - 9x_3 + 2x_4 - 5x_5 = 7, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (9/8, 0, 5/8, 5/4, 0) \end{cases}$$

$$116. \quad \begin{cases} \max(-x_1 - 4x_2 - 5x_3 + 3x_4 - 9x_5) \\ x_1 + 9x_2 + 5x_3 - 4x_4 \leq 1, \\ 3x_1 + 5x_2 + 8x_3 - 8x_4 - 5x_5 \geq 2, \\ -9x_1 + 4x_2 + 3x_3 + 9x_4 - x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (14, 0, 7, 12, 0) \end{cases}$$

$$117. \quad \begin{cases} \max(-8x_1 + 5x_2 + 3x_3 - 4x_4 + 5x_5) \\ -x_1 + 5x_2 + 4x_3 + 2x_4 - x_5 \leq 2, \\ -2x_1 + x_2 - 7x_3 + 8x_4 - 5x_5 \geq 3, \\ 2x_1 - 3x_2 + 2x_3 - 8x_4 + 8x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-3/2, 0, 0, 5/4, 2) \end{cases}$$

$$118. \quad \begin{cases} \max(-4x_1 - 3x_2 + 5x_3 - x_4 + 2x_5) \\ x_1 + 2x_2 - 2x_3 - x_4 + x_5 \leq 7, \\ 2x_1 + 5x_2 - 7x_3 - 3x_4 \geq 5, \\ -x_1 + 4x_2 - 3x_3 + 2x_4 - 3x_5 = 9, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-10, 5, 0, 0, 7) \end{cases}$$

$$119. \quad \begin{cases} \max(-7x_1 - 2x_2 + 5x_3 + 7x_4 + 8x_5) \\ -x_1 - 8x_2 + 6x_3 + 7x_4 + 5x_5 \leq 7, \\ -7x_1 - 8x_2 - 5x_3 + 7x_4 + 4x_5 \geq 5, \\ 4x_1 + 6x_2 + 6x_3 - 6x_4 = 6, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -4, 0, -5, 2) \end{cases}$$

$$120. \quad \begin{cases} \max(-7x_1 - 2x_3 + 4x_4 - 4x_5) \\ 8x_1 - 7x_2 + 7x_3 - 4x_4 - 3x_5 \leq 7, \\ 5x_1 - 2x_2 - 4x_3 - 4x_4 + 4x_5 \geq 8, \\ 7x_1 - 9x_2 - 8x_3 - 8x_4 + 8x_5 = 8, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 8/5, 0, -19/5, -1) \end{cases}$$

$$121. \quad \begin{cases} \max(3x_1 - 9x_2 + 8x_3 - 2x_4 + x_5) \\ 2x_1 - 4x_2 + 6x_3 - 2x_4 + 6x_5 \leq 1, \\ 6x_2 + 8x_3 + 3x_4 + 4x_5 \geq 7, \\ -6x_2 + 8x_3 + 3x_4 + 2x_5 = 8, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (17/6, -1/12, 0, 5/2, 0) \end{cases}$$

$$122. \quad \begin{cases} \max(-3x_1 - 5x_2 + 3x_3 + 5x_4 - 8x_5) \\ 2x_1 - 4x_2 - 5x_3 + 7x_4 - 6x_5 \leq 1, \\ -9x_1 + 3x_2 - 9x_3 + 5x_4 - 7x_5 \geq 4, \\ 4x_1 + 6x_2 - 4x_4 + 6x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 4/3, 5/6, 3/2, 0) \end{cases}$$

$$123. \quad \begin{cases} \max(8x_1 - 7x_2 - 8x_3 - 6x_4 - 8x_5) \\ -9x_1 - 8x_2 - 7x_3 + 5x_4 + 9x_5 \leq 6, \\ -4x_1 - 9x_2 - 6x_3 + 3x_4 + 9x_5 \geq 6, \\ 8x_1 + 4x_2 - 4x_4 + 7x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (6/17, 0, 0, 15/17, 9/17) \end{cases}$$

$$124. \quad \begin{cases} \max(3x_1 - 6x_2 - 8x_3 + 2x_4 + 2x_5) \\ -4x_1 - 8x_2 - 2x_3 - 5x_4 - 6x_5 \leq 6, \\ 7x_1 - 8x_2 - 4x_3 - 7x_4 + 7x_5 \geq 2, \\ 7x_1 - 4x_2 + 7x_3 + 7x_4 + 7x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (2, -1/4, 0, 0, -2) \end{cases}$$

$$125. \quad \begin{cases} \max(2x_1 - 8x_2 + x_3 - 8x_4 - 3x_5) \\ 3x_1 - 3x_2 + 2x_3 + 2x_4 + x_5 \leq 1, \\ 5x_1 + 7x_2 - 6x_3 + 6x_4 - 8x_5 \geq 2, \\ 2x_1 - 5x_2 + 4x_3 + 4x_4 - 8x_5 = 8, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-3/2, 0, 7/12, 13/6, 0) \end{cases}$$

$$126. \quad \begin{cases} \max(8x_1 - 6x_2 + 3x_3 - 3x_4) \\ 9x_1 + 9x_2 - 4x_4 - 9x_5 \leq 9, \\ 6x_1 + 4x_2 - x_3 - 3x_4 \geq 8, \\ 6x_1 - 4x_2 + 8x_3 + 7x_4 + 7x_5 = 9, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (20/17, 4/17, 0, 0, 7/17) \end{cases}$$

$$127. \quad \begin{cases} \max(-4x_1 + 4x_3 - 3x_4) \\ -8x_1 + 9x_2 + 3x_3 + 6x_4 - 9x_5 \leq 9, \\ -7x_1 - 7x_3 + 5x_4 + 2x_5 \geq 9, \\ 2x_1 + 7x_2 - 7x_3 + 2x_4 - 9x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 10/7, 0, 9/7, 9/7) \end{cases}$$



$$128. \quad \begin{cases} \max(5x_2 + 7x_3 + 8x_4 - 4x_5) \\ -8x_1 - 2x_2 - 8x_3 + 2x_4 - 4x_5 \leq 2, \\ -8x_1 - 7x_3 - 5x_4 \geq 8, \\ 8x_1 + 5x_2 - 3x_4 + x_5 = 5, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 1, -3, -4) \end{cases}$$

$$129. \quad \begin{cases} \max(-3x_1 - 2x_2 - 2x_3 - 4x_4 + 2x_5) \\ 6x_1 + 5x_2 + 6x_3 - 2x_4 + 6x_5 \leq 1, \\ -4x_1 - 3x_2 + 8x_3 + 8x_5 \geq 8, \\ -9x_1 - 7x_2 + 9x_3 - 6x_4 + 8x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 8, 5/2, -7) \end{cases}$$

$$130. \quad \begin{cases} \max(8x_1 + 9x_2 + 4x_3 - 4x_4 - x_5) \\ 6x_1 + 6x_2 + 5x_3 + 9x_4 \leq 9, \\ 3x_1 - x_2 + x_3 - 6x_4 + x_5 \geq 4, \\ -x_1 - 5x_2 + 8x_3 - 6x_4 + 7x_5 = 7, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (1, 1/2, 0, 0, 3/2) \end{cases}$$

$$131. \quad \begin{cases} \max(-3x_1 + x_2 - 4x_3 - 6x_4 + 3x_5) \\ -4x_1 - x_2 - 4x_3 - 8x_4 + 5x_5 \leq 9, \\ -2x_1 - 9x_2 + 4x_3 + 5x_4 + x_5 \geq 8, \\ 4x_1 - 7x_2 - 8x_3 - 6x_4 = 8, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -10/11, 0, -3/11, 13/11) \end{cases}$$

$$132. \quad \begin{cases} \max(-9x_1 - 7x_2 - 8x_3 - 6x_4 - x_5) \\ -5x_1 - 2x_2 + 8x_3 + 4x_5 \leq 7, \\ -6x_1 - x_2 + 6x_3 - 8x_4 + 8x_5 \geq 9, \\ -3x_1 + x_2 + x_3 - 3x_4 + 7x_5 = 4, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (3, -17/3, 0, 0, 8/3) \end{cases}$$

$$133. \quad \begin{cases} \max(8x_1 - 2x_3 + 2x_5) \\ -9x_1 - 9x_2 + 8x_3 + 8x_4 - 9x_5 \leq 4, \\ -4x_1 - x_2 - 2x_3 + x_4 - 7x_5 \geq 7, \\ -7x_1 - 9x_2 + 2x_3 + 6x_4 + x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-9/4, 1/4, 0, -7/4, 0) \end{cases}$$

$$134. \quad \begin{cases} \max(-x_1 - 5x_2 - 2x_3 + 8x_4 - 5x_5) \\ -5x_1 - 8x_2 + 6x_3 + 9x_4 + 7x_5 \leq 7, \\ -9x_1 + x_2 + 2x_3 - 2x_4 - 6x_5 \geq 1, \\ -3x_1 - 9x_2 + 3x_3 + 9x_4 + 5x_5 = 6, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -13/17, 10/17, -5/17, 0) \end{cases}$$

$$135. \quad \begin{cases} \max(-7x_1 + 5x_2 - 7x_3 + 3x_4 - 2x_5) \\ -x_1 + 2x_2 - 2x_3 + 4x_4 - 7x_5 \leq 6, \\ -2x_1 - 3x_2 + 7x_3 - 9x_4 - 6x_5 \geq 2, \\ -3x_1 + x_2 - x_3 - x_4 + 2x_5 = 8, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-2, 3, 1, 0, 0) \end{cases}$$

$$136. \quad \begin{cases} \max(x_1 - 4x_2 + x_3 - 2x_4 - 5x_5) \\ 6x_2 + 9x_3 + 9x_4 + 4x_5 \leq 8, \\ -2x_1 + 7x_2 + 7x_3 + 7x_4 + 2x_5 \geq 3, \\ 3x_1 + 3x_2 + x_3 + 9x_4 - x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, -9, 14, 0, -16) \end{cases}$$

$$137. \quad \begin{cases} \max(4x_1 - 4x_2 - 2x_3 - 2x_4 - 8x_5) \\ 7x_2 + 5x_3 - x_4 \leq 6, \\ -6x_1 + 3x_2 + x_3 + 5x_4 + 4x_5 \geq 8, \\ -8x_1 - 8x_2 + 5x_3 - 6x_4 - 2x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (0, 0, 4/3, 2/3, 5/6) \end{cases}$$

$$138. \quad \begin{cases} \max(8x_1 - 9x_2 - 8x_3 + 9x_4 + 2x_5) \\ 8x_1 - 9x_2 + 4x_3 - 2x_4 + 4x_5 \leq 5, \\ -2x_1 + 2x_2 + 2x_3 - 5x_4 + 4x_5 \geq 1, \\ -7x_1 - 7x_2 + 4x_3 - x_4 - 4x_5 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (0, 0, 3/2, 1/3, -1/12) \end{cases}$$

$$139. \quad \begin{cases} \max(-5x_1 - 9x_2 - 4x_3 + 7x_4 + 9x_5) \\ x_1 - 2x_2 + 2x_3 + 7x_4 + 5x_5 \leq 9, \\ 3x_1 + 4x_2 - x_3 + 6x_4 - 9x_5 \geq 5, \\ 3x_1 + 9x_2 + 5x_3 + 6x_4 + 6x_5 = 6, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-9/5, 1/5, 0, 8/5, 0) \end{cases}$$

$$140. \quad \begin{cases} \max(3x_1 + 6x_2 + 2x_3 + 7x_4 - 2x_5) \\ 9x_1 - 5x_3 - 3x_4 + 8x_5 \leq 5, \\ 3x_1 + 9x_2 - 7x_3 + x_4 + 7x_5 \geq 2, \\ -2x_1 + 9x_2 + x_3 + 7x_4 + 5x_5 = 6, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -19/3, -7, 10, 0) \end{cases}$$

$$141. \quad \begin{cases} \max(-x_1 - x_2 - 6x_3 + 4x_4 - 3x_5) \\ 8x_1 + 4x_2 + 6x_3 + 9x_4 + x_5 \leq 3, \\ 6x_1 - 4x_3 - x_4 + 3x_5 \geq 3, \\ -2x_1 - 6x_2 - 5x_3 - x_4 + 2x_5 = 6, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (7/3, -3, 0, 0, -11/3) \end{cases}$$

$$142. \quad \begin{cases} \max(6x_1 + 5x_2 - x_3 - 9x_4 - 2x_5) \\ 3x_1 + x_3 - 6x_4 - 3x_5 \leq 4, \\ 8x_1 - x_2 - 6x_3 - 8x_4 + 6x_5 \geq 9, \\ 5x_1 + 8x_2 - 4x_3 + 7x_4 + 3x_5 = 5, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (3/2, 0, 1, 0, 1/2) \end{cases}$$

$$143. \quad \begin{cases} \max(4x_1 - 9x_2 + 2x_3 - 4x_4 - 5x_5) \\ 4x_1 - 6x_2 + 2x_3 - 9x_4 + 2x_5 \leq 5, \\ x_1 - 2x_2 + 2x_3 + x_4 + 9x_5 \geq 4, \\ 6x_1 - 6x_2 + 2x_3 - x_4 + 4x_5 = 7, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -7/8, 1, 1/4, 0) \end{cases}$$

$$144. \begin{cases} \max(5x_1 + 7x_2 + 3x_3 + 6x_4 + 3x_5) \\ \begin{cases} 3x_1 - 6x_2 - 2x_3 + 2x_5 \leq 5, \\ -5x_1 - 7x_2 - 3x_3 - 2x_4 - 9x_5 \geq 4, \\ 6x_1 + 8x_3 - 4x_4 + 2x_5 = 8, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \end{cases} \\ x = (0, -5/4, 5/4, 1/2, 0) \end{cases}$$

$$145. \begin{cases} \max(9x_1 - 7x_3 + 2x_4 + 4x_5) \\ \begin{cases} -6x_1 + 3x_2 - 3x_3 - 2x_5 \leq 2, \\ -8x_1 - 6x_2 + 5x_3 + 2x_4 + 2x_5 \geq 5, \\ -4x_1 - 9x_2 - 2x_3 - 2x_4 - 8x_5 = 1, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \end{cases} \\ x = (-4/9, 0, 2/9, 1/6, 0) \end{cases}$$

$$146. \begin{cases} \max(5x_1 + x_2 + 9x_3 - 8x_4 + 3x_5) \\ \begin{cases} -4x_1 + 7x_2 + 6x_3 + 3x_4 + 3x_5 \leq 1, \\ -6x_1 - 7x_2 + 8x_3 - 9x_4 + 6x_5 \geq 4, \\ 5x_1 + 3x_2 + 4x_4 + 3x_5 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \end{cases} \\ x = (1/3, 0, -1/3, 0, 13/9) \end{cases}$$

$$147. \begin{cases} \max(-7x_1 + 9x_2 + 6x_3 + 6x_5) \\ \begin{cases} 7x_1 - x_2 + 2x_3 - 2x_4 + 4x_5 \leq 2, \\ 3x_1 + 5x_2 + 2x_3 + 7x_4 - 5x_5 \geq 4, \\ 2x_1 + 4x_2 + 3x_4 + 4x_5 = 2, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \end{cases} \\ x = (0, 2/3, 10/9, -2/9, 0) \end{cases}$$

$$148. \begin{cases} \max(-9x_1 - 4x_2 - 2x_3 - 3x_4 + 6x_5) \\ \begin{cases} -9x_1 - 5x_2 + 3x_3 - x_4 + 8x_5 \leq 7, \\ 5x_1 + 3x_3 + 2x_4 + 2x_5 \geq 6, \\ -3x_1 - 5x_2 + 3x_3 + 2x_4 - 7x_5 = 4, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \end{cases} \\ x = (0, 0, 16/9, 1/9, 2/9) \end{cases}$$

$$149. \begin{cases} \max(2x_1 + 3x_2 + 7x_3 - 9x_4 - 3x_5) \\ \begin{cases} 5x_2 + 5x_3 + 9x_4 + 5x_5 \leq 5, \\ x_1 - 8x_2 + 8x_4 + 4x_5 \geq 6, \\ 4x_1 - 7x_2 + 3x_3 + 3x_4 - 8x_5 = 9, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \end{cases} \\ x = (10/3, 0, 1/3, 0, 2/3) \end{cases}$$

$$150. \begin{cases} \max(-7x_1 - 4x_2 + 6x_3 + 3x_4 + x_5) \\ \begin{cases} 2x_1 + 9x_2 + 2x_4 - 2x_5 \leq 2, \\ x_1 - 9x_2 - x_4 - 3x_5 \geq 2, \\ 5x_1 + 6x_2 - 4x_3 + 4x_4 - 4x_5 = 9, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \end{cases} \\ x = (5, 0, 0, -9/4, 7/4) \end{cases}$$

$$151. \begin{cases} \max(-9x_1 - 9x_2 + 3x_3 - 5x_4 - 9x_5) \\ \begin{cases} 3x_1 - 8x_2 + x_3 - x_4 + 4x_5 \leq 3, \\ -6x_1 - 5x_2 - 9x_3 + x_4 + x_5 \geq 4, \\ -9x_1 + 2x_2 + 4x_3 - 3x_5 = 6, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \end{cases} \\ x = (-17/18, 0, 0, -5/2, 5/6) \end{cases}$$

$$152. \quad \begin{cases} \max(2x_1 - 7x_2 + 2x_3 + x_4 - 9x_5) \\ -6x_1 + 8x_2 + 4x_3 - 3x_4 + 5x_5 \leq 9, \\ -x_2 + 6x_3 - 9x_4 - 2x_5 \geq 5, \\ -8x_1 + 4x_2 - 4x_3 + 6x_4 - 4x_5 = 6, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-7/6, 0, 1/6, -4/9, 0) \end{cases}$$

$$153. \quad \begin{cases} \max(9x_1 - 9x_2 - 3x_3 - 6x_4 - 5x_5) \\ -8x_1 - 5x_2 - 5x_3 + 9x_4 - 9x_5 \leq 8, \\ -4x_1 - 5x_2 + 4x_3 + 9x_4 + 8x_5 \geq 2, \\ -4x_1 + 5x_2 - 4x_3 - 6x_4 - 8x_5 = 6, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-1, 0, 9/2, 0, -5/2) \end{cases}$$

$$154. \quad \begin{cases} \max(x_1 + 2x_2 - 3x_3 - 9x_4 + x_5) \\ 6x_2 + 3x_3 - 2x_4 + 6x_5 \leq 3, \\ -4x_1 - 6x_2 + 6x_3 - 2x_5 \geq 3, \\ -9x_1 - 5x_2 + 3x_3 + 9x_4 - 5x_5 = 2, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-1/2, -1/2, 0, 0, 1) \end{cases}$$

$$155. \quad \begin{cases} \max(-8x_1 + 5x_2 + 4x_3 + 8x_4 - 5x_5) \\ -5x_1 + 8x_2 + 7x_3 + 8x_4 + 8x_5 \leq 8, \\ x_1 - 2x_2 - 5x_3 - 8x_4 - x_5 \geq 3, \\ 7x_1 - 5x_2 + 2x_3 + 8x_4 + 8x_5 = 8, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 0, -4/7, 11/7) \end{cases}$$

$$156. \quad \begin{cases} \max(-7x_1 + 8x_2 - 3x_3 - 8x_4 + 4x_5) \\ 5x_1 + 6x_2 - 5x_3 + 8x_4 \leq 8, \\ -7x_1 - 6x_2 + 9x_3 - 6x_5 \geq 6, \\ 9x_1 - 5x_2 + 5x_3 - 8x_4 + 2x_5 = 6, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, 14, 10, -13/4, 0) \end{cases}$$

$$157. \quad \begin{cases} \max(6x_1 - 2x_2 - 2x_4 - 2x_5) \\ 4x_1 + x_2 - 5x_3 + 6x_4 + 7x_5 \leq 5, \\ 2x_1 + x_2 - 3x_3 - 7x_4 + 2x_5 \geq 3, \\ -2x_1 + x_2 + 4x_3 - 8x_5 = 3, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (7/3, 7/3, 4/3, 0, 0) \end{cases}$$

$$158. \quad \begin{cases} \max(-x_1 + 6x_2 - 4x_3 - 2x_4 + 2x_5) \\ 3x_1 + 4x_2 + 7x_3 - 6x_4 - 2x_5 \leq 9, \\ 7x_1 - 8x_2 - 4x_3 + 2x_4 - 6x_5 \geq 1, \\ x_1 + 4x_2 + 4x_3 + 2x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 11/10, 0, -1/5, -17/10) \end{cases}$$

$$159. \quad \begin{cases} \max(-7x_1 + 7x_2 - 9x_3 - 6x_4 - 5x_5) \\ x_1 + 7x_2 - 5x_3 + 2x_4 - 3x_5 \leq 6, \\ -x_1 + x_2 - 2x_3 + 6x_4 + 7x_5 \geq 8, \\ 4x_1 - 2x_2 - 7x_3 - 3x_4 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (4/3, 7/6, 0, 0, 7/6) \end{cases}$$

$$160. \quad \begin{cases} \max(-2x_1 - x_2 + 2x_3 - 3x_4 + 3x_5) \\ 4x_1 + 5x_2 - 3x_3 + x_4 + 5x_5 \leq 4, \\ -3x_1 - 4x_2 - 9x_3 + 3x_4 + 2x_5 \geq 2, \\ -6x_1 + 9x_2 + 8x_3 - 5x_4 - 3x_5 = 2, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 11/4, 0, 13/2, -13/4) \end{cases}$$

$$161. \quad \begin{cases} \max(6x_1 + 3x_2 + 5x_3 - 8x_4 + 4x_5) \\ -x_1 + 4x_2 + 3x_3 + 6x_4 - 2x_5 \leq 4, \\ 7x_2 + 6x_3 + x_4 - 3x_5 \geq 6, \\ 3x_1 + 4x_2 + 6x_3 + 2x_4 = 1, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-1/3, 1/2, 0, 0, -5/6) \end{cases}$$

$$162. \quad \begin{cases} \max(-8x_1 + 3x_2 + x_3 - 5x_4 - 2x_5) \\ 7x_1 + 3x_2 - 5x_3 + 5x_4 - x_5 \leq 8, \\ 9x_1 - 4x_3 + 6x_4 - 8x_5 \geq 6, \\ -7x_1 + x_2 - x_3 + 4x_4 = 3, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, 1/2, -9/10, 2/5, 0) \end{cases}$$

$$163. \quad \begin{cases} \max(-3x_1 + 8x_2 - 9x_3 - 2x_4 + 9x_5) \\ 7x_1 - 7x_3 + x_4 - x_5 \leq 9, \\ -7x_1 + 6x_2 - 7x_3 + 7x_4 - 7x_5 \geq 9, \\ 7x_1 - 8x_2 + 8x_3 - 9x_4 + 5x_5 = 6, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (19/7, 0, 7/3, 0, -19/3) \end{cases}$$

$$164. \quad \begin{cases} \max(-3x_1 + 6x_2 - 2x_3 - 6x_4 - 2x_5) \\ 5x_1 - 5x_2 + x_3 + 3x_4 - x_5 \leq 3, \\ 5x_1 - 7x_2 - 8x_3 + x_4 - 9x_5 \geq 1, \\ 7x_1 - 5x_2 - 6x_3 + 8x_4 - 6x_5 = 5, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (8/3, 5/3, 0, -2/3, 0) \end{cases}$$

$$165. \quad \begin{cases} \max(6x_2 + 8x_3 + 2x_4 + 9x_5) \\ 5x_1 + 3x_2 + 7x_3 + 2x_4 - 6x_5 \leq 6, \\ 2x_1 + 6x_2 - 2x_3 - 4x_4 - 6x_5 \geq 3, \\ 9x_1 - 7x_2 - 9x_3 - 9x_5 = 8, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (5/4, 1/4, 0, 0, 1/6) \end{cases}$$

$$166. \quad \begin{cases} \max(-x_1 + 4x_2 - 9x_3 - 5x_4 - 9x_5) \\ x_1 + 8x_2 - 7x_3 + 6x_4 - 7x_5 \leq 8, \\ -x_1 - 2x_2 - 5x_3 - 3x_4 - 9x_5 \geq 9, \\ 2x_1 - 6x_2 - 2x_3 + 2x_4 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (11/4, 0, 5/4, 0, -2) \end{cases}$$

$$167. \quad \begin{cases} \max(-8x_1 - 5x_2 - 8x_3 + 4x_4 + 3x_5) \\ -2x_2 - 5x_3 + 6x_4 + 7x_5 \leq 4, \\ -3x_1 - 2x_2 + 6x_3 + 6x_4 - 2x_5 \geq 2, \\ 3x_1 + 4x_2 + 2x_3 - 4x_4 - x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 13/9, 0, 8/9, 2/9) \end{cases}$$

$$168. \quad \begin{cases} \max(-x_1 - 2x_2 + 2x_3 - 7x_4 - 9x_5) \\ -7x_1 + 4x_2 - 2x_3 + 6x_4 - 9x_5 \leq 5, \\ 4x_1 - 7x_3 + 3x_4 - 2x_5 \geq 6, \\ -7x_1 + 4x_2 + x_3 + 7x_4 - 2x_5 = 6, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (3/4, 17/16, 0, 1, 0) \end{cases}$$

$$169. \quad \begin{cases} \max(-8x_1 - 6x_2 - 9x_3 - 4x_4 - 3x_5) \\ -4x_1 - 7x_3 - 4x_4 + x_5 \leq 4, \\ 4x_1 - 6x_2 - 9x_3 - 7x_4 - 6x_5 \geq 3, \\ 4x_1 - 6x_2 - 8x_3 + 5x_4 + 4x_5 = 5, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-9/2, -13/2, 2, 0, 0) \end{cases}$$

$$170. \quad \begin{cases} \max(9x_1 - x_2 + x_3 - 8x_4 - 6x_5) \\ -3x_2 - 5x_4 + 2x_5 \leq 6, \\ 2x_1 - 3x_2 - 6x_3 - 4x_4 + x_5 \geq 3, \\ -3x_1 - 2x_2 + 6x_3 + 3x_4 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (0, 0, -1, 4, 13) \end{cases}$$

$$171. \quad \begin{cases} \max(5x_1 - 5x_2 + 6x_3 + 7x_4 + 5x_5) \\ 6x_1 - 5x_2 + 6x_3 + 9x_4 + 8x_5 \leq 8, \\ 6x_1 - 4x_2 - 6x_3 - 7x_4 + 2x_5 \geq 5, \\ 8x_1 - 6x_2 + 2x_3 + 6x_4 + 4x_5 = 6, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (5/2, 3, 0, 0, 1) \end{cases}$$

$$172. \quad \begin{cases} \max(-6x_1 - 8x_2 - 2x_3 + 4x_4 - 7x_5) \\ 8x_1 + 2x_2 - 8x_3 + 6x_4 + 2x_5 \leq 2, \\ 8x_1 + 8x_2 - 4x_3 + 2x_4 + 7x_5 \geq 5, \\ 8x_1 - 2x_2 + 2x_3 - 5x_4 - 2x_5 = 8, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (11/8, 0, 9/4, 3/2, 0) \end{cases}$$

$$173. \quad \begin{cases} \max(-8x_1 + 9x_2 + 2x_3 + 8x_4 - 8x_5) \\ 7x_2 - x_3 - 4x_4 - 5x_5 \leq 1, \\ x_1 - 7x_2 + 4x_3 - 3x_5 \geq 3, \\ 2x_1 + 3x_2 - 2x_3 - 8x_4 - 8x_5 = 6, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (2, 0, 1/4, -5/16, 0) \end{cases}$$

$$174. \quad \begin{cases} \max(9x_3 + 4x_4 - 8x_5) \\ 4x_1 + x_2 - 6x_3 - 8x_5 \leq 4, \\ 3x_1 - 5x_2 + 6x_3 - 6x_4 - 4x_5 \geq 9, \\ x_1 + 3x_3 - 2x_4 + 5x_5 = 4, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (5/2, 0, 1, 3/4, 0) \end{cases}$$

$$175. \quad \begin{cases} \max(-9x_1 - 4x_2 + 4x_3 - 5x_4 - x_5) \\ -6x_1 + 6x_2 + 8x_3 - 8x_5 \leq 6, \\ -9x_1 + 7x_2 - 4x_3 + 5x_4 - 8x_5 \geq 1, \\ 9x_1 + 2x_2 + 2x_3 - 3x_4 = 5, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (1, -2, 0, 0, -3) \end{cases}$$

$$\begin{aligned}
& \max(-9x_1 + x_2 - 6x_4 - 6x_5) \\
176. \quad & \begin{cases} x_1 + 6x_2 - 4x_3 + 9x_4 + x_5 \leq 2, \\ -8x_1 + 9x_2 - 4x_3 - 4x_4 \geq 2, \\ 8x_1 - 4x_2 - 8x_3 + 5x_4 + 5x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (1/7, 0, -11/14, 0, -9/7) \end{cases} \\
& \max(-6x_1 - 8x_2 - 2x_3 - 5x_4 - 8x_5) \\
177. \quad & \begin{cases} 5x_1 - 2x_2 - 4x_3 - 5x_4 + 2x_5 \leq 4, \\ -7x_1 - 7x_2 - 8x_3 - x_4 - 6x_5 \geq 8, \\ 4x_1 + 4x_2 - 2x_3 + x_4 - 8x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (9, -12, 0, 13, 0) \end{cases} \\
& \max(6x_1 + 3x_2 - 3x_3 - 6x_4 + x_5) \\
178. \quad & \begin{cases} -x_2 + 3x_3 + 9x_4 + 3x_5 \leq 1, \\ -5x_1 - x_2 + 8x_3 + 7x_4 + 3x_5 \geq 6, \\ -x_1 + 9x_2 - 2x_3 + 8x_4 - 4x_5 = 1, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-5/8, 1/8, 3/8, 0, 0) \end{cases} \\
& \max(-6x_1 - 9x_2 - 9x_3 - x_5) \\
179. \quad & \begin{cases} 6x_1 - 3x_3 + 6x_4 + x_5 \leq 3, \\ 9x_1 - 8x_2 - 2x_3 + 3x_5 \geq 5, \\ 6x_1 - 8x_2 - 2x_3 - x_4 - 4x_5 = 8, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (1, 0, 5/7, 0, -6/7) \end{cases} \\
& \max(4x_1 + 8x_2 - 6x_3 + x_4 + 8x_5) \\
180. \quad & \begin{cases} 6x_1 - 7x_2 + 6x_3 + x_4 + 5x_5 \leq 8, \\ -2x_1 - 7x_2 + 5x_3 - 3x_4 + 7x_5 \geq 5, \\ 8x_1 - 4x_2 + 3x_3 + 4x_4 - 7x_5 = 5, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (15/16, -1/2, 0, -9/8, 0) \end{cases} \\
& \max(7x_1 - 8x_2 + 9x_3 - 9x_4 - 6x_5) \\
181. \quad & \begin{cases} 3x_1 + x_2 - 3x_4 + 8x_5 \leq 9, \\ -8x_1 - 2x_3 - x_4 - 8x_5 \geq 1, \\ 5x_1 + 9x_2 - 2x_4 + 3x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -3/5, 11/10, -16/5, 0) \end{cases} \\
& \max(8x_1 - 9x_2 + 8x_3 + 3x_4 - 9x_5) \\
182. \quad & \begin{cases} 2x_1 - 2x_2 - x_3 + 6x_4 - 8x_5 \leq 7, \\ -2x_1 + 3x_2 + 3x_3 - 8x_5 \geq 7, \\ 2x_1 + 4x_2 + 7x_3 + 5x_4 + 5x_5 = 8, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (9/7, 0, 9/7, 0, -5/7) \end{cases} \\
& \max(5x_1 - 2x_2 - 2x_3 + 9x_4 + 5x_5) \\
183. \quad & \begin{cases} -4x_1 + x_2 + 5x_3 + 4x_4 + 2x_5 \leq 4, \\ 4x_1 - 3x_2 + 3x_3 - 7x_4 - 2x_5 \geq 6, \\ 9x_1 - 3x_2 + x_3 + 2x_4 = 9, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-2/3, -5, 0, 0, 19/6) \end{cases}
\end{aligned}$$

$$\begin{aligned}
& \max(-2x_1 + 5x_2 + x_4 + 4x_5) \\
184. \quad & \begin{cases} 8x_1 + 3x_2 + 9x_3 + 7x_4 + 4x_5 \leq 5, \\ -x_1 + 4x_4 - 2x_5 \geq 7, \\ 6x_1 + 2x_3 - 6x_4 + 2x_5 = 8, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (3, 1/3, 0, 0, -5) \end{cases} \\
& \max(6x_1 - 9x_2 - 3x_3 - 6x_4 - 4x_5) \\
185. \quad & \begin{cases} 5x_1 + 3x_2 - 2x_3 - 3x_4 + 3x_5 \leq 2, \\ -6x_1 - 7x_2 + 2x_4 - 8x_5 \geq 6, \\ 8x_1 - 9x_2 + 2x_3 + 4x_4 + 4x_5 = 5, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (1/4, 0, -6, 15/4, 0) \end{cases} \\
& \max(9x_1 - x_2 + 3x_3 + 4x_4 + 2x_5) \\
186. \quad & \begin{cases} 4x_1 - 3x_2 - 2x_3 + 7x_4 - 5x_5 \leq 3, \\ -2x_1 - 7x_2 - 4x_3 + 8x_4 - 6x_5 \geq 8, \\ 8x_1 + 2x_2 + 2x_3 + 9x_4 + 3x_5 = 5, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-10/11, 0, 9/11, 13/11, 0) \end{cases} \\
& \max(-x_1 + 7x_2 + 4x_3 + 7x_4 + 4x_5) \\
187. \quad & \begin{cases} -6x_1 - 2x_2 + 5x_3 + 8x_4 + 2x_5 \leq 3, \\ -5x_1 - 5x_2 - 2x_3 - x_4 + 3x_5 \geq 8, \\ 2x_3 - 5x_4 + 3x_5 = 9, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (13/20, -9/20, 0, 0, 3) \end{cases} \\
& \max(-2x_1 + 7x_2 - 9x_3 + 4x_4 + 8x_5) \\
188. \quad & \begin{cases} x_1 + 7x_2 + 2x_3 - 2x_5 \leq 6, \\ -6x_1 - 6x_2 + 3x_3 - 8x_4 - 3x_5 \geq 9, \\ 3x_1 + 2x_2 - 2x_3 - 5x_5 = 7, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-16, 0, 0, 15, -11) \end{cases} \\
& \max(-6x_3 - 5x_4 - 3x_5) \\
189. \quad & \begin{cases} -5x_1 + 7x_2 - 9x_3 + 7x_4 - 3x_5 \leq 5, \\ -5x_1 - 7x_2 + 5x_3 - 6x_4 + 4x_5 \geq 1, \\ 9x_1 + 9x_2 + 3x_3 - 4x_4 + 2x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (2/7, 0, -11/7, 0, 18/7) \end{cases} \\
& \max(3x_1 + 6x_2 - 4x_3 - 8x_4 + x_5) \\
190. \quad & \begin{cases} 3x_1 - x_2 + 7x_3 + 4x_4 - 4x_5 \leq 2, \\ 2x_1 + 5x_3 - 3x_4 - 3x_5 \geq 1, \\ 3x_1 - 9x_2 + x_3 - 3x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (3, 1/3, 0, 0, 5/3) \end{cases} \\
& \max(9x_1 - 7x_2 + 7x_3 - 8x_5) \\
191. \quad & \begin{cases} 3x_1 + 3x_2 - 2x_4 + 4x_5 \leq 9, \\ -3x_1 - 3x_2 + 3x_3 - 9x_4 - 9x_5 \geq 9, \\ 3x_1 + 9x_2 - 8x_3 - 8x_4 - 2x_5 = 3, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-4, 7, 6, 0, 0) \end{cases}
\end{aligned}$$



$$192. \quad \begin{cases} \max(-9x_1 - 2x_2 - 2x_3 - 9x_4 + 4x_5) \\ -5x_1 + 9x_2 - 2x_3 + 6x_4 + 5x_5 \leq 5, \\ -x_1 - 5x_2 - 4x_3 + 9x_4 + x_5 \geq 7, \\ 7x_1 - 2x_2 - x_4 + 8x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (1/13, 0, 0, 10/13, 2/13) \end{cases}$$

$$193. \quad \begin{cases} \max(-9x_1 - 2x_2 + 5x_3 - 5x_4 - 4x_5) \\ -3x_1 + x_2 + x_3 - 9x_4 - 9x_5 \leq 9, \\ 8x_2 - 6x_3 + 9x_4 + 2x_5 \geq 4, \\ -8x_1 + 3x_2 - 4x_3 - 9x_4 - 7x_5 = 9, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (0, 11/17, -2/17, 0, -16/17) \end{cases}$$

$$194. \quad \begin{cases} \max(3x_1 + 6x_3 + 9x_4 + 4x_5) \\ -3x_1 - 3x_2 + 9x_3 + 4x_4 + 3x_5 \leq 4, \\ -x_1 - 9x_2 + 6x_3 - 9x_4 \geq 6, \\ 3x_1 - 9x_2 + 8x_4 - 2x_5 = 4, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-1/6, -1/2, 2/9, 0, 0) \end{cases}$$

$$195. \quad \begin{cases} \max(-5x_1 + x_2 + 6x_3 + 4x_4 + 3x_5) \\ x_1 - 8x_2 + 7x_3 - 4x_4 + 4x_5 \leq 6, \\ -3x_1 - 5x_2 - 9x_3 - 4x_4 + 9x_5 \geq 6, \\ 2x_1 + 2x_2 - 8x_3 + x_4 + 9x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, -5/12, 0, -5/12, 1/4) \end{cases}$$

$$196. \quad \begin{cases} \max(-x_1 - 5x_2 + 8x_4 + 8x_5) \\ 2x_2 + 9x_3 + x_4 - 9x_5 \leq 9, \\ 8x_1 - 2x_2 - 6x_3 - 9x_4 - 6x_5 \geq 6, \\ 6x_2 - 3x_3 + 8x_4 + 5x_5 = 7, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (9, 0, 6, 0, 5) \end{cases}$$

$$197. \quad \begin{cases} \max(-3x_1 - 8x_2 - 5x_3 + 2x_4 - 4x_5) \\ -2x_1 - 6x_2 - 4x_3 - 4x_4 + 5x_5 \leq 1, \\ -3x_1 - 3x_2 + 9x_5 \geq 4, \\ -4x_1 - 2x_2 - 7x_4 + 5x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 5/12, -1/9, 4/9) \end{cases}$$

$$198. \quad \begin{cases} \max(5x_1 + 8x_2 + 7x_3 - x_4 + 2x_5) \\ x_1 + 6x_2 - 2x_3 + 5x_4 + 6x_5 \leq 1, \\ -4x_1 + 4x_2 - 9x_3 - 5x_4 + 4x_5 \geq 3, \\ -4x_1 + 8x_2 + 2x_3 - 2x_4 + 2x_5 = 5, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-1/2, 5/12, 0, 0, -1/6) \end{cases}$$

$$199. \quad \begin{cases} \max(-8x_1 + 8x_2 + x_3 + 5x_4 + 2x_5) \\ -5x_1 - 3x_3 + 8x_4 + x_5 \leq 4, \\ 2x_3 - 2x_4 - 8x_5 \geq 4, \\ -7x_2 - 7x_3 + 8x_4 + 5x_5 = 1, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (13, 0, 17, 15, 0) \end{cases}$$

$$200. \quad \begin{cases} \max(-6x_1 + 9x_2 - 5x_3 + 2x_4 + 5x_5) \\ \begin{cases} 9x_2 - 3x_3 + 8x_4 \leq 9, \\ 6x_1 - 4x_2 - 6x_3 + 8x_4 - 8x_5 \geq 5, \\ -3x_1 + 2x_2 + x_4 - x_5 = 5, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-7/6, 0, 0, 9/8, -3/8) \end{cases} \end{cases}$$

$$201. \quad \begin{cases} \max(-5x_1 + 5x_2 + 7x_3 + 7x_4 - 3x_5) \\ \begin{cases} -9x_1 + 8x_2 + 9x_3 + 9x_4 - x_5 \leq 3, \\ -5x_1 - 8x_2 + 7x_3 - 2x_4 + 2x_5 \geq 9, \\ -8x_1 + 8x_2 - 2x_3 + x_4 + 5x_5 = 8, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-7/6, 0, 1/6, -1, 0) \end{cases} \end{cases}$$

$$202. \quad \begin{cases} \max(-3x_2 - 5x_3 - 9x_4 - 3x_5) \\ \begin{cases} -8x_1 - 6x_2 - 8x_3 - 9x_4 + 6x_5 \leq 5, \\ -8x_1 + 4x_2 - 4x_3 - 9x_4 - 4x_5 \geq 7, \\ 9x_2 - x_4 + 2x_5 = 9, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (5/8, 1, -2, 0, 0) \end{cases} \end{cases}$$

$$203. \quad \begin{cases} \max(-5x_1 - 9x_2 - 5x_3 + 3x_4 - 3x_5) \\ \begin{cases} -8x_1 + 6x_3 + 4x_4 + 4x_5 \leq 4, \\ -x_1 + x_2 - 2x_3 - 2x_4 + 3x_5 \geq 1, \\ -5x_1 - 5x_3 + x_4 - x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 8, 0, 2, -1) \end{cases} \end{cases}$$

$$204. \quad \begin{cases} \max(-4x_1 - 5x_2 - 4x_3 - 9x_4) \\ \begin{cases} -x_1 - 4x_2 + 6x_3 + 9x_4 + 3x_5 \leq 5, \\ 4x_1 - 2x_2 + 6x_3 - x_4 \geq 4, \\ 3x_1 - 2x_2 + 5x_3 + 9x_4 - x_5 = 2, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (1/2, 0, 1/3, 0, 7/6) \end{cases} \end{cases}$$

$$205. \quad \begin{cases} \max(-8x_1 + 3x_2 - 9x_3 + 9x_4 + 4x_5) \\ \begin{cases} 6x_1 + 5x_2 - x_3 - 2x_5 \leq 2, \\ -5x_1 - 9x_2 - x_4 - 3x_5 \geq 3, \\ -x_1 + 9x_2 - 3x_3 - 7x_4 - 7x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (0, 0, 1/2, 3/4, -5/4) \end{cases} \end{cases}$$

$$206. \quad \begin{cases} \max(-4x_1 + 7x_2 + 6x_3 + x_4 - 5x_5) \\ \begin{cases} 9x_1 - x_2 - 6x_3 - 5x_4 - 6x_5 \leq 6, \\ -4x_1 - 6x_2 + 5x_3 + 7x_4 - 2x_5 \geq 6, \\ 7x_1 - 7x_3 - 9x_4 - 3x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (3/16, -15/16, 0, 0, -9/16) \end{cases} \end{cases}$$

$$207. \quad \begin{cases} \max(8x_1 - 4x_2 + x_3 - 2x_4 - 4x_5) \\ \begin{cases} 6x_1 - x_2 + 4x_3 - 2x_4 - 5x_5 \leq 2, \\ 2x_1 - 2x_3 - 8x_4 - 4x_5 \geq 9, \\ 2x_1 + x_2 - 2x_3 + 6x_4 - 9x_5 = 7, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (3/2, 17/2, 0, -3/4, 0) \end{cases} \end{cases}$$

$$208. \quad \begin{cases} \max(x_1 + 6x_2 - 2x_3 + 3x_4 - 3x_5) \\ -2x_1 - 8x_2 - 7x_3 + 3x_4 + 7x_5 \leq 5, \\ -8x_1 - 7x_2 - 2x_3 + 3x_4 + 6x_5 \geq 2, \\ 3x_1 - 4x_2 - 6x_3 - 6x_4 - 8x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 0, -1/2, -2/3, 1/2) \end{cases}$$

$$209. \quad \begin{cases} \max(5x_1 + 5x_2 - 7x_3 + 7x_4 + 3x_5) \\ 9x_1 - 2x_2 + 4x_3 - 3x_4 - x_5 \leq 2, \\ 4x_1 - 9x_2 - 8x_3 - 5x_4 + 9x_5 \geq 9, \\ 9x_1 + 7x_2 - 8x_3 + 3x_4 + 5x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 0, 7/12, -1/3, 4/3) \end{cases}$$

$$210. \quad \begin{cases} \max(-5x_1 + 9x_2 + 3x_3 + 6x_4 - 2x_5) \\ -4x_1 + 6x_2 + 3x_3 + 6x_4 - 8x_5 \leq 5, \\ -8x_2 - 6x_3 + 4x_5 \geq 8, \\ 2x_1 - 3x_2 - 3x_3 - 3x_4 + 8x_5 = 6, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-11/2, 0, 1/9, 0, 13/6) \end{cases}$$

$$211. \quad \begin{cases} \max(8x_3 + x_4 + 3x_5) \\ -6x_1 + 9x_2 + 6x_3 - 2x_4 - 3x_5 \leq 3, \\ 7x_1 - 7x_2 - x_3 - 7x_4 + x_5 \geq 7, \\ 7x_1 - 5x_2 - x_3 + 5x_4 + 5x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (4/3, 0, 4/3, 0, -1) \end{cases}$$

$$212. \quad \begin{cases} \max(2x_1 - 4x_2 - 8x_3 - 9x_4 - 4x_5) \\ 9x_1 + 7x_2 - 9x_3 - 5x_4 - 4x_5 \leq 7, \\ -5x_1 + 3x_2 - x_3 + 4x_4 - 8x_5 \geq 7, \\ -2x_2 + 3x_3 + 9x_4 - 7x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 5/3, 2/3, 0, -1/3) \end{cases}$$

$$213. \quad \begin{cases} \max(-8x_1 + 4x_2 - 9x_3 - 6x_4 + 2x_5) \\ -2x_1 + 4x_2 + 6x_3 - 5x_4 - 3x_5 \leq 2, \\ -2x_1 - 8x_2 - 9x_3 - 5x_4 - 7x_5 \geq 9, \\ -4x_1 - 9x_2 - 9x_3 + 8x_4 = 4, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (1/6, 0, 0, 7/12, -7/4) \end{cases}$$

$$214. \quad \begin{cases} \max(4x_1 - 3x_2 - x_3 + 9x_4 + 2x_5) \\ 4x_1 + 9x_3 - 2x_4 + x_5 \leq 1, \\ x_1 + 3x_2 + 5x_3 + x_4 + 6x_5 \geq 4, \\ -7x_1 + x_2 + 9x_4 + 4x_5 = 2, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (1/2, 1, 0, 1/2, 0) \end{cases}$$

$$215. \quad \begin{cases} \max(-2x_1 - 4x_2 - 8x_3 - 6x_4 + 9x_5) \\ 7x_1 + 4x_2 - 6x_3 - 2x_4 + x_5 \leq 2, \\ -7x_1 + 2x_2 + 2x_3 - 3x_4 - 2x_5 \geq 8, \\ 9x_1 - 2x_2 + 6x_3 + 8x_4 - x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 5/2, 13/10, 0, -1/5) \end{cases}$$

$$216. \quad \begin{cases} \max(x_1 - 4x_2 + 4x_3 + x_4 + 6x_5) \\ -4x_1 + 6x_2 + 4x_3 + 3x_4 - x_5 \leq 1, \\ x_1 - 3x_2 - x_3 + 3x_4 - 2x_5 \geq 8, \\ 4x_1 + 5x_2 - 2x_3 + 5x_5 = 5, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (11/10, 0, -3/10, 11/5, 0) \end{cases}$$

$$217. \quad \begin{cases} \max(2x_1 - 6x_2 + 8x_3 + 8x_4 - x_5) \\ 3x_1 + 6x_2 + 7x_3 + 9x_5 \leq 5, \\ 9x_2 - 2x_3 - 3x_4 \geq 6, \\ x_1 - 6x_2 - 9x_3 - 2x_4 + 2x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (1, 1/3, 0, -1, 0) \end{cases}$$

$$218. \quad \begin{cases} \max(5x_1 - 6x_2 - 3x_3 - 9x_4 + 4x_5) \\ x_1 - 3x_2 + 2x_3 + 2x_4 \leq 9, \\ -6x_2 + 2x_3 + 8x_4 + 2x_5 \geq 8, \\ 3x_1 - 3x_2 + x_3 - 9x_4 - 9x_5 = 5, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (7, -2/3, 0, 0, 2) \end{cases}$$

$$219. \quad \begin{cases} \max(-2x_1 + 9x_2 + 9x_3 - 3x_5) \\ 4x_1 + 3x_2 + 4x_3 + 3x_4 + 3x_5 \leq 7, \\ 8x_1 - 7x_2 - 6x_3 + x_4 - 5x_5 \geq 5, \\ -2x_1 - 3x_2 - 4x_3 - 2x_4 + 9x_5 = 2, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (9/2, 19, -17, 0, 0) \end{cases}$$

$$220. \quad \begin{cases} \max(6x_2 + 3x_3 + x_4 + 2x_5) \\ -6x_1 + 5x_2 + 3x_3 + 3x_4 + 4x_5 \leq 4, \\ 2x_1 - 5x_2 - 6x_3 - 5x_4 - 2x_5 \geq 2, \\ 8x_1 - 4x_2 - 4x_3 - 4x_4 + 7x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 19/8, -3/4, -15/8, 0) \end{cases}$$

$$221. \quad \begin{cases} \max(-3x_1 + 3x_2 - 4x_3 - 6x_4 - x_5) \\ 2x_1 - 7x_2 + 8x_3 - 5x_4 + 9x_5 \leq 2, \\ -6x_1 + 6x_2 - 8x_3 + 6x_4 + 8x_5 \geq 6, \\ 4x_1 - 7x_2 - 7x_3 - 3x_4 - 7x_5 = 6, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-5/7, -17/7, 0, 19/7, 0) \end{cases}$$

$$222. \quad \begin{cases} \max(-7x_1 + 6x_2 - 5x_3 + 2x_4 - 9x_5) \\ 4x_1 - 5x_2 + 9x_3 + 9x_4 + 4x_5 \leq 3, \\ 7x_1 - 9x_2 + 2x_3 + 4x_4 + 7x_5 \geq 6, \\ -2x_1 + 5x_2 - 8x_3 + 4x_4 - x_5 = 1, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-13, -3, 0, 0, 10) \end{cases}$$

$$223. \quad \begin{cases} \max(-5x_1 + 9x_2 + 9x_3 - 2x_4 - 8x_5) \\ -2x_1 + 9x_2 - 8x_3 - 2x_4 - 7x_5 \leq 1, \\ -4x_1 - 9x_2 - 7x_3 + 3x_4 - 8x_5 \geq 9, \\ -4x_1 + 5x_2 + x_3 + 3x_4 + x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (7/8, 0, -7/8, 17/8, 0) \end{cases}$$

$$224. \quad \begin{cases} \max(-9x_1 + 8x_2 + 2x_3 - 3x_4 - 3x_5) \\ 4x_1 + 8x_2 + 2x_3 + 4x_4 + 2x_5 \leq 9, \\ -6x_1 - x_2 + 6x_4 + 3x_5 \geq 3, \\ -3x_1 + 4x_2 + 6x_3 + x_4 + 8x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 7/2, 9/5, -13/5) \end{cases}$$

$$225. \quad \begin{cases} \max(2x_1 + 3x_2 + 5x_3 - 9x_4 - 6x_5) \\ 4x_1 + 6x_2 + 8x_3 + 7x_4 + 2x_5 \leq 4, \\ 4x_1 + 8x_2 - 9x_3 + x_4 + 6x_5 \geq 8, \\ 2x_2 + 3x_3 + 5x_4 + x_5 = 7, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-9/2, 4, 0, 0, -1) \end{cases}$$

$$226. \quad \begin{cases} \max(3x_1 - 3x_2 - 6x_3 + 5x_4 - 4x_5) \\ -3x_1 - 4x_2 - 2x_3 + 4x_4 - 9x_5 \leq 1, \\ 4x_1 + 2x_2 - 9x_3 + x_4 - 5x_5 \geq 7, \\ -4x_1 - 2x_2 + 4x_3 - 2x_4 - 4x_5 = 3, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-5, 9/2, -2, 0, 0) \end{cases}$$

$$227. \quad \begin{cases} \max(-8x_1 + 6x_2 - 3x_3 - 8x_4 - 8x_5) \\ 5x_1 - 7x_2 + 8x_3 - x_4 + 8x_5 \leq 3, \\ 2x_1 + 2x_2 - 2x_3 - 2x_4 + 6x_5 \geq 3, \\ -2x_1 + 8x_2 - 8x_3 - 3x_4 + 8x_5 = 4, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 3/5, 7/10, -8/5, 0) \end{cases}$$

$$228. \quad \begin{cases} \max(2x_1 + 5x_2 + 8x_3 - 3x_4 + 3x_5) \\ 6x_1 + 7x_2 + 3x_3 - x_4 - 5x_5 \leq 9, \\ 9x_1 - 3x_2 + x_4 - 7x_5 \geq 6, \\ -6x_1 + 4x_2 + 3x_3 - x_4 - 9x_5 = 7, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 7, 19/2, 1/2) \end{cases}$$

$$229. \quad \begin{cases} \max(-2x_1 + 3x_2 - 7x_3 - 7x_4 - 5x_5) \\ 4x_1 + 8x_2 + 6x_4 - 6x_5 \leq 9, \\ -9x_1 - 3x_2 + 5x_4 - 9x_5 \geq 6, \\ x_1 - 8x_2 + x_3 + 7x_4 - 3x_5 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 0, -6, 15/8, 3/8) \end{cases}$$

$$230. \quad \begin{cases} \max(-9x_1 - 3x_2 - 3x_3 - 7x_4 + 2x_5) \\ -2x_1 + 6x_2 - 2x_3 + x_4 + 2x_5 \leq 3, \\ 9x_1 - 3x_3 + 2x_4 - 9x_5 \geq 7, \\ -7x_1 + 2x_2 + 5x_3 + 3x_4 + 9x_5 = 4, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (1/9, 0, -4/9, 7/3, 0) \end{cases}$$

$$231. \quad \begin{cases} \max(-2x_1 + 6x_2 + 3x_3 + 6x_4 + 7x_5) \\ -2x_1 - 5x_3 - 6x_4 \leq 5, \\ -5x_1 - 5x_2 - 9x_3 + 6x_4 + x_5 \geq 9, \\ x_1 + x_2 + 5x_3 + 6x_4 + 6x_5 = 1, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-11/3, 7/3, 0, 7/18, 0) \end{cases}$$

$$232. \quad \begin{cases} \max(7x_3 - 6x_2 - 8x_4 + 2x_5) \\ 3x_1 + 4x_2 - 5x_3 \leq 8, \\ -2x_1 - 8x_2 + 4x_3 - 5x_4 + 4x_5 \geq 9, \\ -5x_1 - 9x_2 - 7x_3 + 5x_4 - 2x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 0, -8/5, -1, 13/5) \end{cases}$$

$$233. \quad \begin{cases} \max(6x_1 - 5x_2 - x_3 + 4x_4 + 9x_5) \\ 2x_1 + 3x_2 + 3x_3 + 8x_4 + x_5 \leq 5, \\ 4x_1 + 7x_2 + 8x_3 + 6x_4 - 7x_5 \geq 7, \\ -4x_1 + 7x_2 + 5x_3 + 8x_4 + x_5 = 9, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (0, 8/15, 14/15, 0, 3/5) \end{cases}$$

$$234. \quad \begin{cases} \max(7x_1 + 8x_2 - 3x_3 + 4x_4 + 2x_5) \\ 5x_1 - 8x_2 + 9x_3 + 9x_4 - 8x_5 \leq 4, \\ -8x_1 - 7x_2 - 6x_3 - 4x_5 \geq 5, \\ -5x_1 - x_2 - 7x_3 - x_5 = 5, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-4/5, 9/5, 0, 0, -14/5) \end{cases}$$

$$235. \quad \begin{cases} \max(-8x_1 + 8x_2 + 9x_3 + 8x_4 + 5x_5) \\ 5x_1 + 6x_2 - 3x_4 \leq 8, \\ -8x_1 - 6x_2 - 7x_3 - 8x_4 - 6x_5 \geq 7, \\ x_1 - 6x_2 - x_3 - 5x_4 - 8x_5 = 7, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 1/3, 1, -2, 0) \end{cases}$$

$$236. \quad \begin{cases} \max(-2x_1 - 8x_2 - 4x_3 - 6x_4 - 4x_5) \\ -3x_2 - 4x_3 - 6x_4 + 3x_5 \leq 9, \\ -9x_1 - 2x_3 - 3x_4 + 3x_5 \geq 3, \\ 7x_1 + 6x_4 - 7x_5 = 8, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -1, -7/2, 4/3, 0) \end{cases}$$

$$237. \quad \begin{cases} \max(7x_1 + x_2 - 7x_3 + 4x_4 + 8x_5) \\ 8x_1 + 3x_2 - 7x_3 + 6x_4 - 2x_5 \leq 1, \\ -5x_1 + 4x_3 - 8x_4 + 4x_5 \geq 7, \\ -x_2 + 5x_3 + 3x_4 + 6x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 13/2, 3, 0, -5/4) \end{cases}$$

$$238. \quad \begin{cases} \max(x_1 - 6x_2 - x_3 - 7x_4 - 9x_5) \\ 9x_2 - 2x_3 + 5x_4 - 2x_5 \leq 8, \\ 6x_1 - 9x_2 + 3x_3 + 9x_4 - 3x_5 \geq 3, \\ -6x_1 - x_2 - 6x_3 + 3x_4 + 4x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (3/4, 0, -9/4, 0, -7/4) \end{cases}$$

$$239. \quad \begin{cases} \max(-7x_1 - 5x_2 + 9x_3 - 5x_4 + 6x_5) \\ 2x_1 + 7x_2 - x_3 + 5x_4 + x_5 \leq 5, \\ 8x_1 - 3x_2 - 6x_3 - 4x_4 - 4x_5 \geq 4, \\ x_1 - 2x_2 - 7x_3 + 4x_4 - x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (13/12, 0, 0, 5/12, 3/4) \end{cases}$$

$$\begin{aligned}
& \max(-8x_1 - x_2 - x_3 + 9x_4 + 3x_5) \\
240. \quad & \begin{cases} x_1 - 3x_2 + 9x_3 \leq 6, \\ 5x_1 - 9x_2 + 7x_3 - 6x_4 \geq 3, \\ 7x_1 - 6x_2 + 5x_3 + 4x_4 - 9x_5 = 7, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, -2, 0, 5/2, 5/3) \end{cases} \\
& \max(-8x_1 - x_2 - 5x_3 - x_4 - 8x_5) \\
241. \quad & \begin{cases} -4x_1 - x_2 + 5x_3 + 9x_4 - 8x_5 \leq 1, \\ 8x_1 + 2x_2 + 8x_3 - 6x_4 - 5x_5 \geq 7, \\ -4x_1 - 3x_2 + 7x_3 - 9x_4 - 8x_5 = 3, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (1/2, -1/2, 1/2, 0, 0) \end{cases} \\
& \max(3x_1 + 4x_2 + x_3 + 6x_4 - 5x_5) \\
242. \quad & \begin{cases} 5x_1 - 8x_2 + 3x_4 + 3x_5 \leq 9, \\ -4x_1 - 8x_2 - 3x_3 - 8x_4 + 3x_5 \geq 2, \\ 9x_1 - 9x_3 - 8x_4 - 9x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, -17/8, 7/3, 0, -8/3) \end{cases} \\
& \max(9x_1 - 8x_2 - 4x_3 + 8x_4 - 9x_5) \\
243. \quad & \begin{cases} 3x_1 + x_2 + 5x_4 + 9x_5 \leq 7, \\ x_1 + 6x_2 - 2x_3 + 4x_4 - 5x_5 \geq 6, \\ 2x_1 - x_2 + 7x_3 + 8x_4 + x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (8/7, 0, -1, 5/7, 0) \end{cases} \\
& \max(-9x_1 - x_2 - 3x_3 - 8x_4 + x_5) \\
244. \quad & \begin{cases} 9x_1 - x_2 - x_3 + 3x_4 + 3x_5 \leq 1, \\ 7x_1 + 4x_2 - 9x_3 + 4x_4 + 6x_5 \geq 6, \\ -8x_1 + 7x_2 + 6x_3 + 4x_4 + 3x_5 = 6, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (1/7, 13/14, 0, 0, 3/14) \end{cases} \\
& \max(-x_1 - 4x_2 + 2x_3 - 3x_4 - 2x_5) \\
245. \quad & \begin{cases} -x_1 - 3x_2 + 7x_3 - 3x_4 - x_5 \leq 2, \\ -4x_1 - 8x_2 - 5x_3 + 7x_4 \geq 9, \\ -x_1 - x_2 + 4x_3 + 9x_4 + x_5 = 6, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 1/10, 0, 7/5, -13/2) \end{cases} \\
& \max(-4x_1 - 3x_2 + 6x_3 - 9x_4 + 4x_5) \\
246. \quad & \begin{cases} 9x_1 + 3x_2 + 6x_3 + 3x_4 + 5x_5 \leq 7, \\ 9x_1 - 6x_2 + 6x_3 + 6x_4 + 5x_5 \geq 5, \\ 7x_1 + 8x_2 - x_3 - 6x_4 - 2x_5 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 4, -2/3, -3) \end{cases} \\
& \max(8x_1 + 5x_2 - 5x_3 - 5x_4 - 4x_5) \\
247. \quad & \begin{cases} -x_1 + 6x_2 + 8x_3 + 3x_4 - 2x_5 \leq 6, \\ -3x_1 - 2x_2 + 3x_4 - 3x_5 \geq 2, \\ -3x_1 + 3x_2 + 2x_3 - 6x_4 + 7x_5 = 3, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -13/7, 16/7, 0, 4/7) \end{cases}
\end{aligned}$$

$$248. \quad \begin{cases} \max(2x_1 + x_2 - 3x_3 - 5x_4 - x_5) \\ -2x_1 + 4x_2 + 8x_3 + x_4 - 8x_5 \leq 8, \\ 5x_1 - 3x_3 + 9x_4 - 4x_5 \geq 9, \\ -7x_1 + 4x_2 - 6x_3 - 8x_4 - 8x_5 = 2, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (6/5, 11/10, 0, 0, -3/4) \end{cases}$$

$$249. \quad \begin{cases} \max(-3x_1 - x_2 - 6x_3 + 6x_4 + 2x_5) \\ 3x_1 - 7x_2 + x_3 + 6x_4 + 4x_5 \leq 3, \\ 2x_1 - 4x_3 + 3x_4 - 5x_5 \geq 9, \\ -2x_1 + 8x_2 - 3x_4 + 8x_5 = 7, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (1, 2, 0, 7/3, 0) \end{cases}$$

$$250. \quad \begin{cases} \max(-9x_1 + 4x_2 - 6x_3 - 3x_4) \\ 6x_1 + 5x_2 + 2x_3 - 2x_4 + 3x_5 \leq 3, \\ 7x_1 + 8x_2 - 4x_3 + 9x_4 - 3x_5 \geq 3, \\ -4x_1 + 3x_2 - 9x_3 + 5x_4 - 3x_5 = 3, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, 2/5, -2/5, 0, 3/5) \end{cases}$$

$$251. \quad \begin{cases} \max(-5x_1 - 3x_2 - 2x_3 - x_4 - 2x_5) \\ -3x_1 + 8x_3 + 6x_5 \leq 3, \\ 3x_1 + 8x_2 + 2x_3 - 7x_4 - 3x_5 \geq 3, \\ -6x_1 - x_2 - 7x_3 + 2x_4 + x_5 = 5, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-1, 5/9, 0, -2/9, 0) \end{cases}$$

$$252. \quad \begin{cases} \max(4x_1 + 5x_2 + x_3 + 9x_4 - 3x_5) \\ 5x_1 + 2x_2 + 2x_3 + 5x_4 + 8x_5 \leq 3, \\ -2x_1 - 8x_2 - 6x_4 - 3x_5 \geq 7, \\ x_1 - 6x_2 + 4x_3 - 8x_4 - 5x_5 = 5, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -11/7, 3/4, 13/14, 0) \end{cases}$$

$$253. \quad \begin{cases} \max(-3x_1 + 7x_2 + 7x_3 - 5x_4 - 4x_5) \\ 8x_1 - 7x_2 + 7x_3 - 3x_4 + 5x_5 \leq 4, \\ 7x_1 - 6x_2 - 4x_3 - 7x_5 \geq 8, \\ 8x_1 - 2x_2 - 7x_3 - 3x_4 + 7x_5 = 4, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (8/7, 0, 0, 12/7, 0) \end{cases}$$

$$254. \quad \begin{cases} \max(-x_1 + 6x_2 - 6x_3 - 5x_4 - 5x_5) \\ -7x_1 + 6x_2 + 4x_3 - 5x_4 - 4x_5 \leq 3, \\ -3x_1 - 9x_2 + 6x_3 - 9x_4 - 2x_5 \geq 9, \\ -3x_1 - x_2 - 3x_3 - x_5 = 2, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-7/3, 0, 0, -4/3, 5) \end{cases}$$

$$255. \quad \begin{cases} \max(6x_1 + 4x_2 - 5x_3 - 4x_4 - 4x_5) \\ x_1 + 4x_2 + 6x_3 + 9x_4 \leq 6, \\ -4x_1 - 5x_2 - 4x_3 + 3x_4 + 4x_5 \geq 6, \\ -x_1 - 9x_2 - 9x_3 + 6x_4 = 7, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-9/5, 0, 0, 13/15, -19/20) \end{cases}$$



$$256. \quad \begin{cases} \max(5x_1 + 3x_3 + 9x_4 - 7x_5) \\ -8x_1 - 3x_2 + 6x_3 + 9x_4 - 3x_5 \leq 3, \\ -2x_1 - x_2 + 6x_3 - 6x_4 - 7x_5 \geq 8, \\ 5x_1 + 5x_3 = 8, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, 2, 8/5, -1/15, 0) \end{cases}$$

$$257. \quad \begin{cases} \max(7x_1 + 5x_2 - 6x_3 - 3x_4 + 5x_5) \\ 3x_1 + 6x_2 - 3x_3 + x_5 \leq 1, \\ -7x_2 + 6x_3 - x_4 - 4x_5 \geq 7, \\ -6x_2 - x_3 + x_4 - 7x_5 = 8, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (10/3, 0, 3, 11, 0) \end{cases}$$

$$258. \quad \begin{cases} \max(-4x_1 - 6x_2 + 8x_4 + 7x_5) \\ -2x_1 - 9x_2 - 3x_3 + 4x_4 + 4x_5 \leq 6, \\ -3x_1 - 9x_2 - 6x_3 - 7x_4 - 5x_5 \geq 7, \\ -2x_1 - 4x_3 + 7x_4 - 8x_5 = 1, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (1/2, -11/18, -1/2, 0, 0) \end{cases}$$

$$259. \quad \begin{cases} \max(3x_1 - 8x_2 + 3x_3 + 5x_4 - 7x_5) \\ 6x_1 + 9x_2 + x_3 + 4x_4 - 4x_5 \leq 2, \\ -2x_1 + 7x_2 - 2x_3 - 3x_4 + 4x_5 \geq 4, \\ 8x_1 + 2x_2 + x_3 - 5x_4 - 2x_5 = 7, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (9/7, 0, -6/7, 0, 17/14) \end{cases}$$

$$260. \quad \begin{cases} \max(7x_1 + 2x_2 - 6x_3 - 7x_4 + 3x_5) \\ 2x_1 + 8x_2 + 5x_3 + x_4 - 3x_5 \leq 3, \\ -5x_2 + 2x_3 - x_4 + 6x_5 \geq 9, \\ 4x_2 + 6x_3 + 8x_4 - 6x_5 = 5, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 7/6, 0, 13/6, 17/6) \end{cases}$$

$$261. \quad \begin{cases} \max(2x_1 - 8x_2 - 9x_3 - x_4 + x_5) \\ -9x_1 - 8x_2 + 6x_3 - 2x_4 + 7x_5 \leq 5, \\ -5x_1 + 7x_2 + 7x_3 - 6x_4 - 4x_5 \geq 6, \\ -9x_1 - 3x_2 + 4x_3 + x_5 = 8, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, 4/7, 17/7, 5/2, 0) \end{cases}$$

$$262. \quad \begin{cases} \max(3x_1 + 8x_2 - 4x_3 - 3x_4 + 4x_5) \\ 4x_1 + 9x_2 + x_3 - 9x_4 - 9x_5 \leq 8, \\ -8x_2 + 2x_3 - 9x_4 - 9x_5 \geq 6, \\ -4x_1 + 5x_2 + x_3 + 2x_5 = 8, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (1/2, 0, 0, -17/3, 5) \end{cases}$$

$$263. \quad \begin{cases} \max(-2x_1 - 8x_2 - 2x_3 + 5x_4 + x_5) \\ -9x_1 + 6x_2 + 5x_3 + 2x_4 + 8x_5 \leq 4, \\ -8x_1 + 5x_2 + 6x_3 + 6x_4 + 8x_5 \geq 4, \\ 4x_1 - 5x_2 - 2x_3 - 4x_4 - 6x_5 = 2, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (1, 0, 3, -1, 0) \end{cases}$$

$$264. \begin{cases} \max(5x_1 + 2x_2 - 2x_3 + 8x_4 + 3x_5) \\ \begin{cases} -4x_1 + 9x_2 - 9x_3 - 2x_4 - x_5 \leq 7, \\ -6x_1 - 9x_2 - 2x_3 - 8x_4 - 2x_5 \geq 8, \\ 2x_1 - 2x_2 + 2x_4 + 7x_5 = 5, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \end{cases} \\ x = (-9/4, 0, 0, 3/8, 5/4) \end{cases}$$

$$265. \begin{cases} \max(-9x_1 + 3x_2 - 5x_3 - 9x_4 - 7x_5) \\ \begin{cases} -2x_1 + 9x_3 - 6x_4 + 5x_5 \leq 5, \\ -4x_1 - 3x_2 - 2x_3 + 5x_5 \geq 1, \\ x_2 + 9x_3 + 8x_4 - 6x_5 = 9, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \end{cases} \\ x = (-4, 5, 0, 1/2, 0) \end{cases}$$

$$266. \begin{cases} \max(5x_1 - 4x_2 + 8x_3 + 2x_4 - 2x_5) \\ \begin{cases} 9x_1 + 6x_2 - 9x_3 - 4x_4 + 6x_5 \leq 3, \\ 4x_1 - 6x_2 - 6x_3 - 7x_4 + 8x_5 \geq 8, \\ -2x_1 + 7x_2 - 7x_3 - 4x_5 = 8, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \end{cases} \\ x = (-7/5, 0, -6/5, 0, 4/5) \end{cases}$$

$$267. \begin{cases} \max(-4x_1 - 7x_2 - 8x_3 - 7x_4 - 9x_5) \\ \begin{cases} 3x_2 + x_4 - 2x_5 \leq 3, \\ 6x_1 - 8x_2 + 6x_3 - 3x_4 - 7x_5 \geq 6, \\ x_1 + 2x_2 + 2x_3 - 4x_4 - 5x_5 = 1, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \end{cases} \\ x = (17/3, 1, -10/3, 0, 0) \end{cases}$$

$$268. \begin{cases} \max(-7x_1 - x_2 - 9x_3 - 8x_4 - 5x_5) \\ \begin{cases} -x_1 + 2x_2 + 5x_3 - 3x_4 + x_5 \leq 5, \\ -2x_1 + 4x_2 - 4x_3 + 3x_4 - 5x_5 \geq 1, \\ -8x_1 + x_2 + 7x_3 - 3x_4 + 3x_5 = 6, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \end{cases} \\ x = (0, 19/7, -4/7, 0, 17/7) \end{cases}$$

$$269. \begin{cases} \max(-6x_1 - 9x_2 - 2x_3 + 9x_4 - 9x_5) \\ \begin{cases} x_1 - 6x_2 + x_3 + 2x_4 + 4x_5 \leq 9, \\ 3x_1 - 6x_2 - 5x_4 - 3x_5 \geq 8, \\ -3x_1 + 9x_2 + x_3 - 2x_4 + 8x_5 = 3, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \end{cases} \\ x = (4, 2/3, 9, 0, 0) \end{cases}$$

$$270. \begin{cases} \max(9x_1 - 7x_2 - 2x_3 + 3x_4 - 9x_5) \\ \begin{cases} -6x_1 - x_3 - 5x_4 + 2x_5 \leq 2, \\ -2x_1 - 5x_2 - 9x_3 - x_4 + x_5 \geq 9, \\ -7x_1 + 6x_2 - 8x_3 - 7x_4 + 3x_5 = 4, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \end{cases} \\ x = (-1, 0, 0, 6, 13) \end{cases}$$

$$271. \begin{cases} \max(-5x_1 - 9x_2 + 4x_3 - 9x_4 - 7x_5) \\ \begin{cases} -5x_1 - 3x_2 + 9x_3 - 9x_4 - x_5 \leq 6, \\ -8x_1 + 3x_2 + 3x_3 - 3x_4 + 2x_5 \geq 5, \\ -7x_1 - x_2 + 9x_3 - 3x_4 = 5, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \end{cases} \\ x = (0, 3/4, 1/2, -5/12, 0) \end{cases}$$

$$\begin{aligned}
& \max(8x_1 - 8x_2 + 4x_3 - 8x_4 - x_5) \\
272. & \begin{cases} 8x_1 + 2x_2 + 6x_3 + 3x_4 + x_5 \leq 6, \\ 6x_1 + 9x_2 + 4x_3 + 3x_4 - 8x_5 \geq 2, \\ 6x_1 + 4x_2 - 2x_3 + 2x_4 + 9x_5 = 2, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (12/19, -6/19, 5/19, 0, 0) \end{cases} \\
& \max(-x_1 - x_2 + 6x_3 + x_5) \\
273. & \begin{cases} 6x_1 - 4x_2 - 2x_3 - 4x_4 + 5x_5 \leq 1, \\ -3x_1 - 3x_2 - 7x_3 + 4x_4 + 2x_5 \geq 3, \\ x_1 + 2x_2 + 3x_3 - 3x_4 - 4x_5 = 4, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 7/2, -19/6, -13/6, 0) \end{cases} \\
& \max(5x_2 + x_3 + 5x_4 - 8x_5) \\
274. & \begin{cases} -x_1 - 5x_2 - 2x_3 - x_4 + 4x_5 \leq 9, \\ -x_1 - 9x_2 - 3x_3 - 5x_4 - 8x_5 \geq 5, \\ -6x_1 - 3x_2 + 2x_3 + x_4 - x_5 = 9, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (2/5, -13/5, 0, 18/5, 0) \end{cases} \\
& \max(-x_2 + x_3 - 5x_4 - 7x_5) \\
275. & \begin{cases} -x_1 - x_2 + 2x_3 - 9x_4 \leq 5, \\ -4x_1 + 3x_2 + 4x_3 - 8x_4 - x_5 \geq 2, \\ 3x_1 - x_2 + 5x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (2/3, 0, -1/6, -2/3, 0) \end{cases} \\
& \max(8x_1 + 8x_2 - 2x_3 - 3x_4 - 5x_5) \\
276. & \begin{cases} 9x_1 - 3x_2 - 8x_3 + 9x_4 + 9x_5 \leq 8, \\ 2x_1 + x_2 + 2x_3 - 3x_4 + 2x_5 \geq 9, \\ -x_1 + 2x_2 + 7x_3 - 3x_4 - 2x_5 = 8, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (4, 13/3, 0, 0, -5/3) \end{cases} \\
& \max(-8x_1 + x_2 - 8x_3 + 3x_4 - x_5) \\
277. & \begin{cases} -3x_1 - 7x_2 - 3x_3 + 5x_5 \leq 2, \\ 2x_1 - 6x_2 - 2x_3 + 3x_4 + 4x_5 \geq 1, \\ 8x_1 - 4x_2 - 2x_3 + 3x_4 + 6x_5 = 2, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 1/2, -11/6, 1/9, 0) \end{cases} \\
& \max(-4x_1 - 5x_2 - 7x_3 + 6x_4 - 8x_5) \\
278. & \begin{cases} 3x_1 + 8x_2 - 3x_3 + 3x_4 \leq 6, \\ -x_1 - 9x_2 - 7x_3 + 3x_4 + x_5 \geq 4, \\ -4x_1 - 6x_2 + 9x_3 - 4x_4 + x_5 = 5, \\ x_1 \geq 0, x_2 \geq 0, x_3 \geq 0, \\ x = (0, 0, 5/3, 11/3, 14/3) \end{cases} \\
& \max(-6x_1 + 5x_2 - 5x_3 + 8x_5) \\
279. & \begin{cases} 6x_2 + x_3 + 7x_4 + 5x_5 \leq 8, \\ x_1 - 2x_2 + x_3 + 4x_4 + 3x_5 \geq 4, \\ -2x_1 - x_2 + 3x_3 - 4x_4 - 5x_5 = 8, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-2, 0, 3, 0, 1) \end{cases}
\end{aligned}$$

$$280. \quad \begin{cases} \max(9x_2 + 2x_3 - 4x_4 + x_5) \\ -3x_1 + 4x_2 + 9x_3 - 3x_4 + 3x_5 \leq 9, \\ -8x_2 - 2x_3 - 9x_4 - 9x_5 \geq 6, \\ x_1 + 9x_2 - 4x_3 - 6x_4 - 4x_5 = 5, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (17, 0, 6, -2, 0) \end{cases}$$

$$281. \quad \begin{cases} \max(4x_1 + 5x_2 + 5x_3 - 8x_5) \\ x_1 + x_2 + 2x_4 - x_5 \leq 5, \\ 4x_1 + 4x_2 + x_3 - 5x_4 \geq 5, \\ -2x_1 - 4x_2 - 2x_3 + x_4 - 2x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (3/4, 0, 2, 0, -17/4) \end{cases}$$

$$282. \quad \begin{cases} \max(8x_1 - 7x_2 + x_3 - 5x_4 - 3x_5) \\ 2x_1 - 3x_2 + 6x_3 - 8x_4 + 3x_5 \leq 1, \\ 9x_1 + x_2 + 6x_3 - 7x_4 - 6x_5 \geq 5, \\ 4x_1 + 8x_2 - 5x_3 + 7x_4 + x_5 = 3, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (3/4, 0, -7/4, -5/4, 0) \end{cases}$$

$$283. \quad \begin{cases} \max(-8x_1 - 3x_2 + 2x_4 - 9x_5) \\ 3x_1 - x_3 + 3x_4 - x_5 \leq 3, \\ 2x_1 + 4x_2 + x_3 - 3x_4 + 2x_5 \geq 5, \\ -7x_1 - x_2 - 2x_3 + 4x_4 + 5x_5 = 6, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 2, -6, -1, 0) \end{cases}$$

$$284. \quad \begin{cases} \max(2x_1 - 9x_2 + x_3 - 6x_4) \\ 4x_1 - x_2 + 2x_3 - 3x_4 + 2x_5 \leq 1, \\ -9x_1 + x_2 + 6x_3 + 3x_4 + x_5 \geq 9, \\ -3x_1 + 7x_2 - 2x_3 + x_4 - 9x_5 = 2, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, 3/5, 5/4, 3/10, 0) \end{cases}$$

$$285. \quad \begin{cases} \max(4x_1 + x_3 - 3x_4 - 5x_5) \\ 7x_1 - 2x_2 - 9x_3 + x_4 - x_5 \leq 4, \\ -7x_1 - 8x_2 - 8x_3 - 3x_4 + 9x_5 \geq 4, \\ -x_1 + 7x_2 - 2x_3 + 4x_4 - 9x_5 = 1, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (0, 5/19, -10/19, 0, 4/19) \end{cases}$$

$$286. \quad \begin{cases} \max(8x_1 - x_2 + 3x_3) \\ 9x_1 - 9x_2 - x_3 + 2x_4 - 8x_5 \leq 8, \\ -6x_1 - x_2 - 7x_3 - 6x_5 \geq 7, \\ 6x_1 - 2x_2 - 6x_3 + 2x_4 - 7x_5 = 8, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (1/9, -2/3, -1, 0, 0) \end{cases}$$

$$287. \quad \begin{cases} \max(-9x_1 - 9x_2 - 8x_3) \\ x_1 + 6x_2 + 5x_3 - 6x_4 \leq 7, \\ -9x_1 + 9x_2 + 7x_3 + 2x_4 + 4x_5 \geq 3, \\ -x_1 + 6x_2 + 7x_3 - 8x_4 - 8x_5 = 2, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (0, 1/6, 0, -1, 7/8) \end{cases}$$

$$288. \quad \begin{cases} \max(-x_1 + 3x_2 - 6x_3 - 7x_4 - 5x_5) \\ -2x_1 + 7x_2 - 2x_3 + 9x_4 + 5x_5 \leq 4, \\ -4x_1 - 6x_2 - 7x_3 + 5x_4 - 2x_5 \geq 5, \\ 2x_1 - 7x_2 - 9x_3 - 5x_4 - 9x_5 = 4, \\ x_1 \geq 0, x_2 \geq 0, x_5 \geq 0, \\ x = (0, 0, -16/15, -1/5, 11/15) \end{cases}$$

$$289. \quad \begin{cases} \max(7x_1 + 3x_2 + 3x_4 + x_5) \\ 8x_1 + 9x_3 + 7x_4 + 4x_5 \leq 5, \\ -5x_1 + 9x_3 + 3x_4 - 9x_5 \geq 7, \\ -9x_1 - 6x_2 + 4x_3 - 7x_4 - x_5 = 6, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (-2/13, -4/13, 9/13, 0, 0) \end{cases}$$

$$290. \quad \begin{cases} \max(3x_1 - 9x_2 + 4x_3 - 6x_4 - 9x_5) \\ -4x_1 + 5x_2 + 7x_3 + 3x_4 - x_5 \leq 9, \\ -2x_1 + 7x_3 - 6x_4 \geq 3, \\ -9x_1 + 7x_2 + 2x_3 + 3x_5 = 8, \\ x_1 \geq 0, x_2 \geq 0, x_4 \geq 0, \\ x = (0, 8/7, 3/7, 0, -2/7) \end{cases}$$

$$291. \quad \begin{cases} \max(-5x_1 - 6x_2 + 5x_3 - 5x_4) \\ 4x_1 + 6x_2 + 6x_3 - 2x_5 \leq 7, \\ 6x_1 - 5x_2 + 4x_3 - 6x_4 - 4x_5 \geq 5, \\ 2x_2 - 5x_3 + 9x_4 - 6x_5 = 7, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-19/10, 0, 8/5, 0, -5/2) \end{cases}$$

$$292. \quad \begin{cases} \max(-6x_1 + x_3 + 2x_4 - 4x_5) \\ -x_1 + 5x_2 - 6x_3 - 2x_4 + 4x_5 \leq 9, \\ 8x_1 - x_2 - 9x_3 + x_4 - 2x_5 \geq 1, \\ 4x_1 - 2x_2 - 6x_3 + 4x_4 + 7x_5 = 5, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (1/6, 17/6, 0, 5/2, 0) \end{cases}$$

$$293. \quad \begin{cases} \max(9x_1 + 3x_2 + 9x_4 + 9x_5) \\ -9x_1 + 7x_2 + 4x_3 + x_4 + 7x_5 \leq 1, \\ -7x_1 - 7x_2 + x_4 + 5x_5 \geq 1, \\ x_1 + 7x_2 - 6x_3 + 9x_4 + x_5 = 1, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (1/18, 0, -1/9, 0, 5/18) \end{cases}$$

$$294. \quad \begin{cases} \max(-8x_1 - 2x_2 - x_3 + 6x_4 + 6x_5) \\ 7x_1 + 7x_2 + 3x_3 - 3x_4 + 7x_5 \leq 7, \\ 9x_1 + 3x_2 + 6x_3 - 9x_4 + 3x_5 \geq 7, \\ -7x_1 - 6x_2 + 6x_3 + 4x_4 - 2x_5 = 2, \\ x_3 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (2/3, -11/6, 0, 0, 13/6) \end{cases}$$

$$295. \quad \begin{cases} \max(4x_1 + 7x_2 - 5x_3 + 3x_4 - 8x_5) \\ 9x_1 + 2x_2 + 4x_3 - 2x_4 + 4x_5 \leq 4, \\ -3x_1 + 9x_2 + 4x_3 + 3x_4 + 9x_5 \geq 3, \\ 3x_1 - 3x_2 + 5x_3 - 3x_4 + 2x_5 = 6, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -3/16, 9/8, 1/16, 0) \end{cases}$$

$$296. \quad \begin{cases} \max(7x_1 - 6x_2 + 8x_3 + 5x_4) \\ -2x_2 + 4x_3 + x_4 + 5x_5 \leq 8, \\ 7x_1 + 2x_2 + 8x_3 - 6x_4 - 5x_5 \geq 5, \\ -8x_1 - 8x_2 - 4x_3 + 8x_4 - x_5 = 8, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (17/3, -4/3, 0, 16/3, 0) \end{cases}$$

$$297. \quad \begin{cases} \max(8x_1 + 8x_2 - 3x_3 + 8x_4 - 2x_5) \\ 6x_1 + 7x_2 - 7x_3 + x_4 - 5x_5 \leq 5, \\ 6x_1 - 5x_2 - 8x_3 - x_4 - 4x_5 \geq 1, \\ -6x_1 - 9x_2 - 8x_3 - x_4 - x_5 = 7, \\ x_2 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (-1, 0, 0, 1, -2) \end{cases}$$

$$298. \quad \begin{cases} \max(-8x_1 - 6x_2 - 4x_3 - 6x_4 + x_5) \\ 9x_2 - 5x_3 + 8x_4 \leq 7, \\ -4x_1 + 9x_2 - 4x_3 - 2x_4 - 9x_5 \geq 5, \\ 8x_1 - x_3 + 5x_4 - x_5 = 3, \\ x_2 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (1/4, 2/9, -1, 0, 0) \end{cases}$$

$$299. \quad \begin{cases} \max(-3x_1 - 6x_2 - 6x_3 + x_4 + 3x_5) \\ -8x_1 + 2x_2 - 6x_3 - 4x_4 - 8x_5 \leq 1, \\ -4x_1 + 5x_2 + x_3 - 9x_4 - 6x_5 \geq 4, \\ 4x_1 + 9x_2 + 2x_3 - 2x_4 + 5x_5 = 8, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, 17/20, 1/20, 0, 1/20) \end{cases}$$

$$300. \quad \begin{cases} \max(-4x_1 - 5x_2 + 3x_3 + 7x_4 - 9x_5) \\ -8x_1 - 3x_2 - 9x_3 - 7x_4 - 5x_5 \leq 7, \\ -8x_1 - 7x_2 - 3x_3 + 2x_4 - 6x_5 \geq 4, \\ 7x_1 + 8x_2 - 3x_3 - 7x_4 - 2x_5 = 1, \\ x_1 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (4, -6, 0, -3, 0) \end{cases}$$

$$301. \quad \begin{cases} \max(x_1 + x_2 + 3x_3 - 6x_4 + x_5) \\ 3x_1 + x_3 - 8x_4 + 4x_5 \leq 9, \\ x_1 + 3x_2 - 7x_3 - 5x_4 + 2x_5 \geq 6, \\ 2x_1 - 8x_2 - x_4 + 2x_5 = 3, \\ x_2 \geq 0, x_3 \geq 0, x_5 \geq 0, \\ x = (-3, 0, 0, 0, 9/2) \end{cases}$$

$$302. \quad \begin{cases} \max(2x_1 + 2x_2 - 6x_3 + 3x_4 + 4x_5) \\ -4x_1 - 7x_3 + 3x_5 \leq 9, \\ -9x_1 - 9x_2 - 7x_3 - 9x_5 \geq 3, \\ -8x_1 + x_2 - 5x_3 - 3x_4 + 3x_5 = 3, \\ x_1 \geq 0, x_3 \geq 0, x_4 \geq 0, \\ x = (0, -10/3, 0, 8/9, 3) \end{cases}$$

$$303. \quad \begin{cases} \max(-4x_2 - 9x_3 - 6x_4 - 2x_5) \\ 2x_1 - 8x_2 + 9x_3 + x_4 + 3x_5 \leq 7, \\ -2x_1 - 2x_2 + 6x_3 + x_5 \geq 3, \\ 5x_1 - 8x_2 - x_4 + 5x_5 = 5, \\ x_1 \geq 0, x_4 \geq 0, x_5 \geq 0, \\ x = (0, -5/13, 4/13, 0, 5/13) \end{cases}$$

$$\begin{array}{l}
 \max(-x_1 - 6x_3 - 8x_4 - 6x_5) \\
 \mathbf{304.} \quad \left\{ \begin{array}{l}
 -2x_1 + 8x_2 + 6x_3 - 8x_4 + 3x_5 \leq 9, \\
 2x_3 - 2x_4 - 4x_5 \geq 1, \\
 x_1 + 2x_2 - 3x_3 + 9x_4 + 6x_5 = 5, \\
 x_1 \geq 0, \quad x_4 \geq 0, \quad x_5 \geq 0, \\
 x = (10/3, 19/12, 1/2, 0, 0)
 \end{array} \right.
 \end{array}$$